

# Distributed Phased Arrays:

## Coordinating Wireless Systems at the Wavelength Level and Their Application to Communications and Sensing

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**delta**  
Distributed Electromagnetics  
Theory and Applications

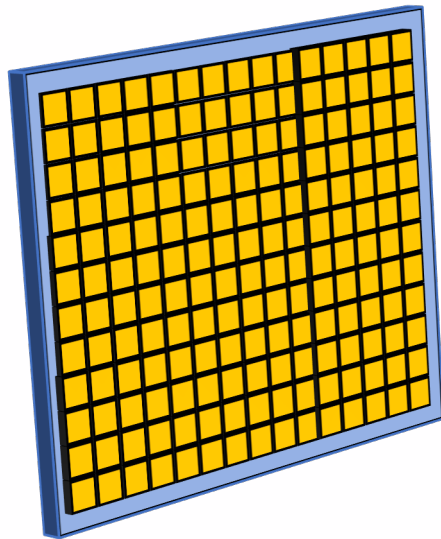


**emrg**  
Electromagnetics Research Group  
Michigan State University

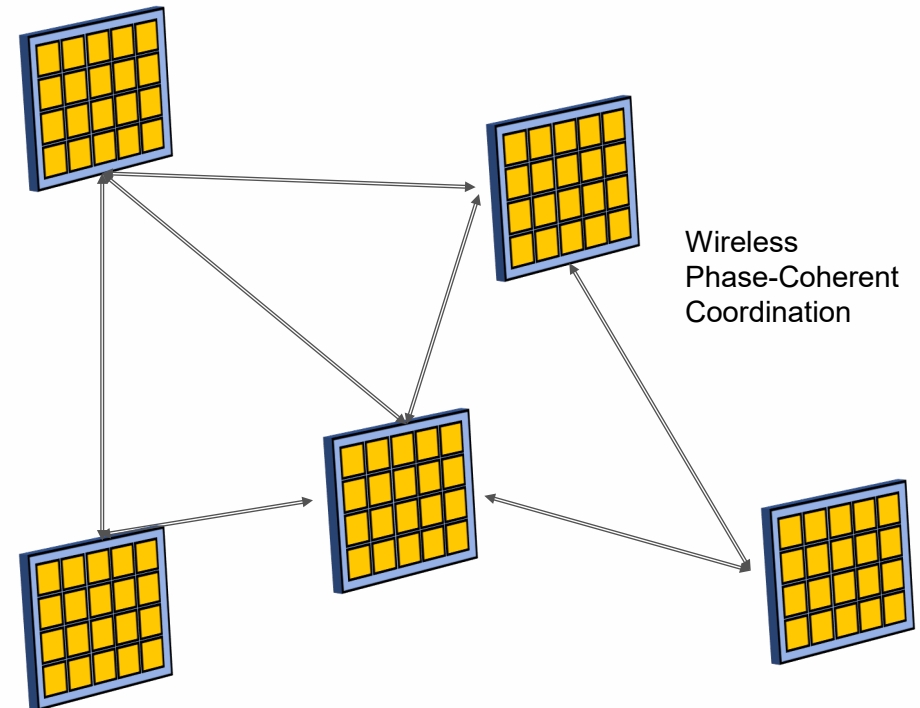
# Distributed Phased Arrays



Traditional Single-Platform  
Phased Array



Distributed Array

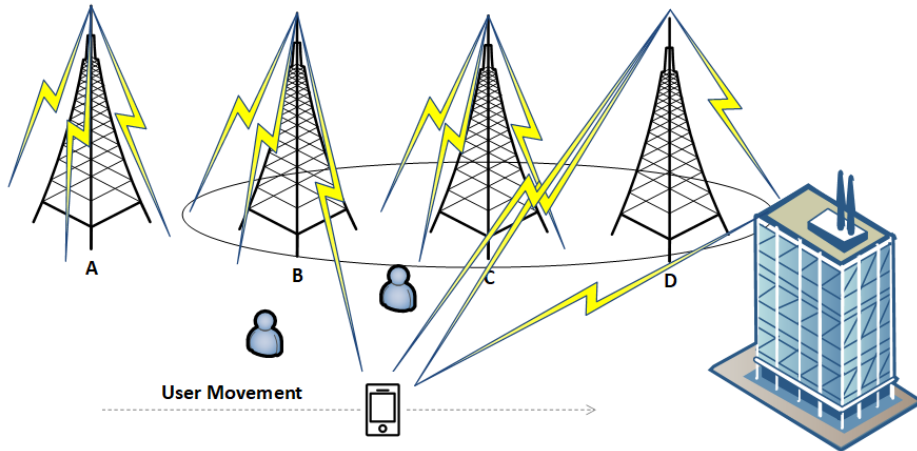




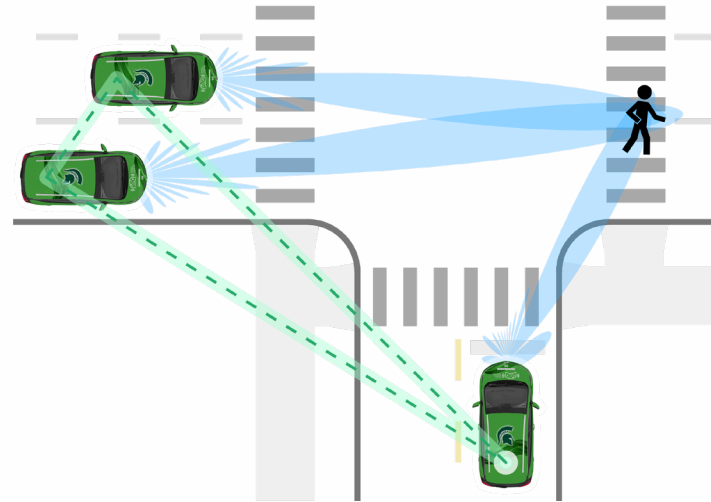
# Applications

Develop technologies supporting coordination of the spatioelectrical states of networked wireless systems

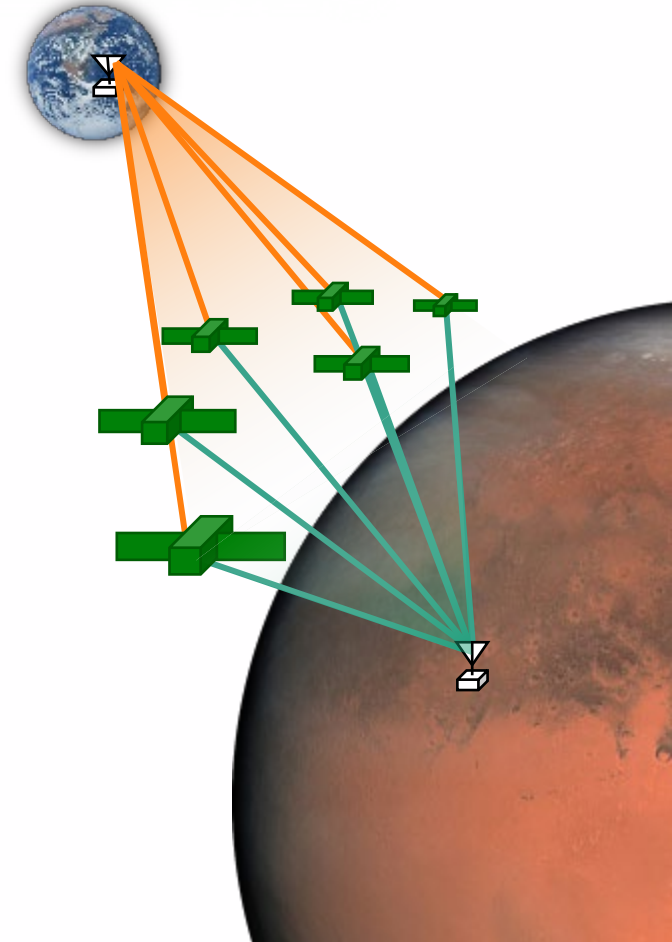
*5G/6G Communication*



*V2X Sensing and Communication*



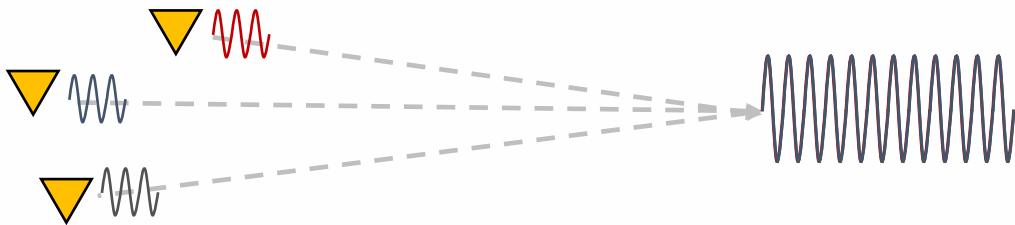
*Space Communication and Remote Sensing*



# Coordination



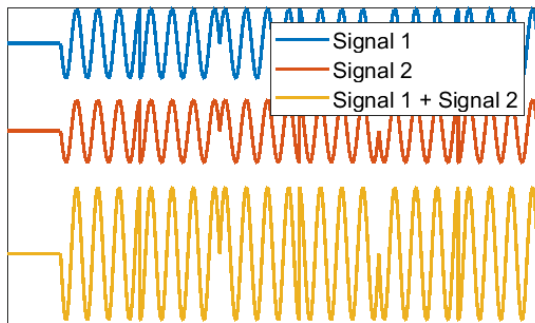
Alignment of the electrical states of the array nodes



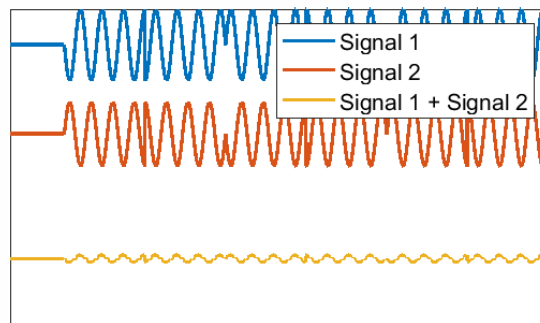
$$\mathbf{J} = \hat{\mathbf{z}} e^{-j\omega t} \sum_n I_n \delta l_n \delta(x - dx_n) \delta(y - dy_n) \delta(z - dz_n)$$

$$\mathbf{E} = \hat{\boldsymbol{\theta}} j k \eta \sin \theta \frac{e^{-jk r}}{4\pi r} \sum_{n=1}^N I_n \delta l_n e^{-j\omega t} e^{j \frac{2\pi}{\lambda} d_n \cos \theta_n}$$

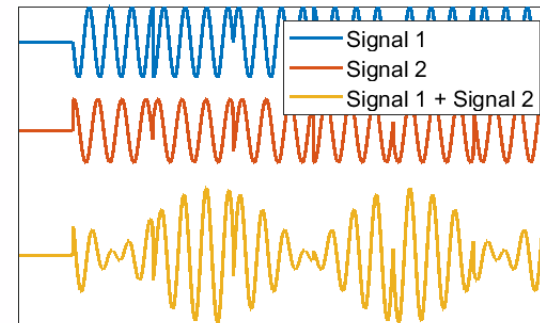
$$s_r(t) = \sum_{n=1}^N h_n \alpha_n (t - \delta t_n) e^{j[2\pi(f + \delta f_n)(t - \delta t_n) + \phi_n]}$$



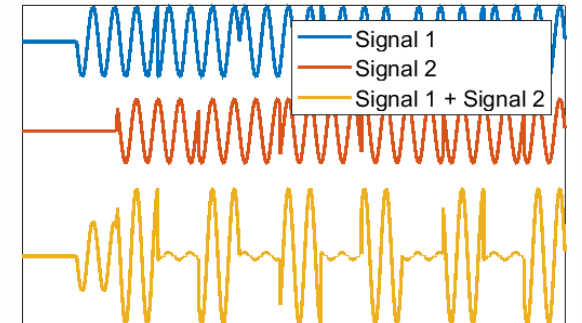
Ideal summation



w/o phase coherence



w/o frequency synchronization



w/o time synchronization

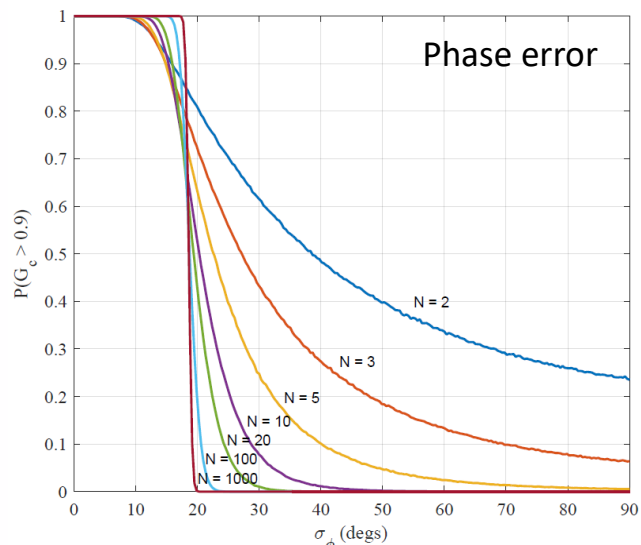
# Error Tolerance



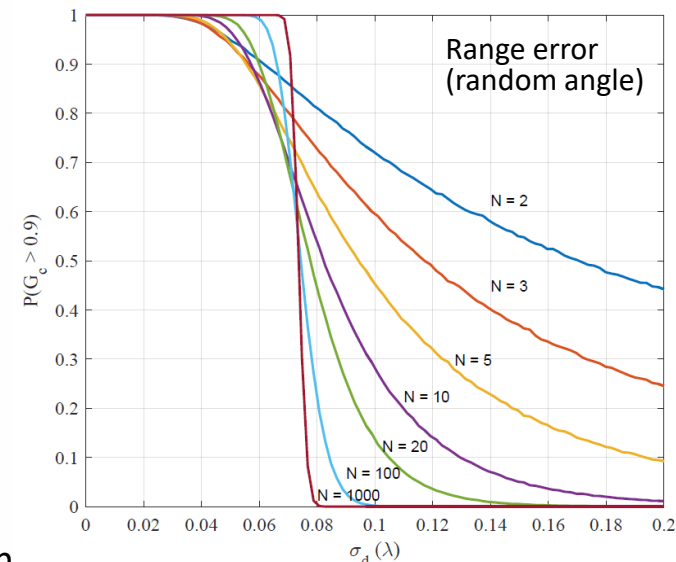
Beamforming signal relative to ideal

$$s_i(t) = C \sum e^{j(2\pi ft + \frac{2\pi}{\lambda} d_n \cos\theta_n)}$$

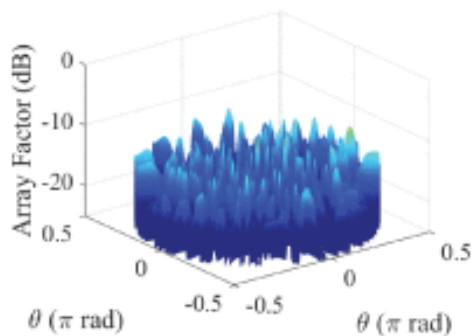
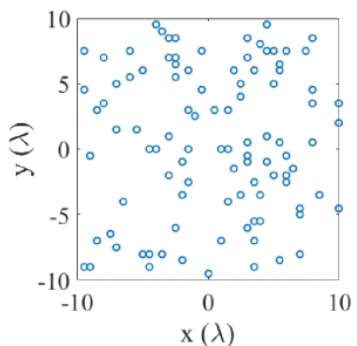
$$G_c = \frac{|s_r s_r^*|}{|s_i s_i^*|}$$



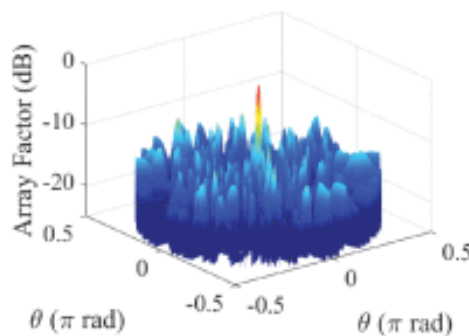
Phase errors  $< 18^\circ$  for 90% coherent gain



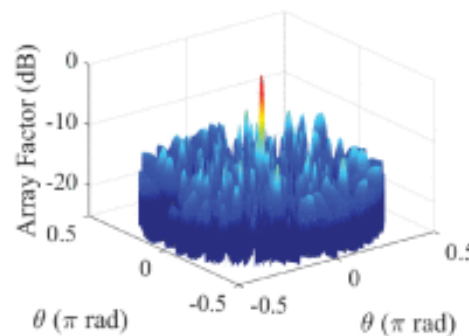
Internode range errors  $< \lambda/15$  for 90% coherent gain



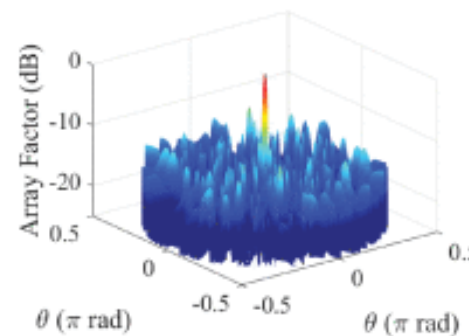
Phase error:  $180^\circ$



Phase error:  $90^\circ$



Phase error:  $36^\circ$

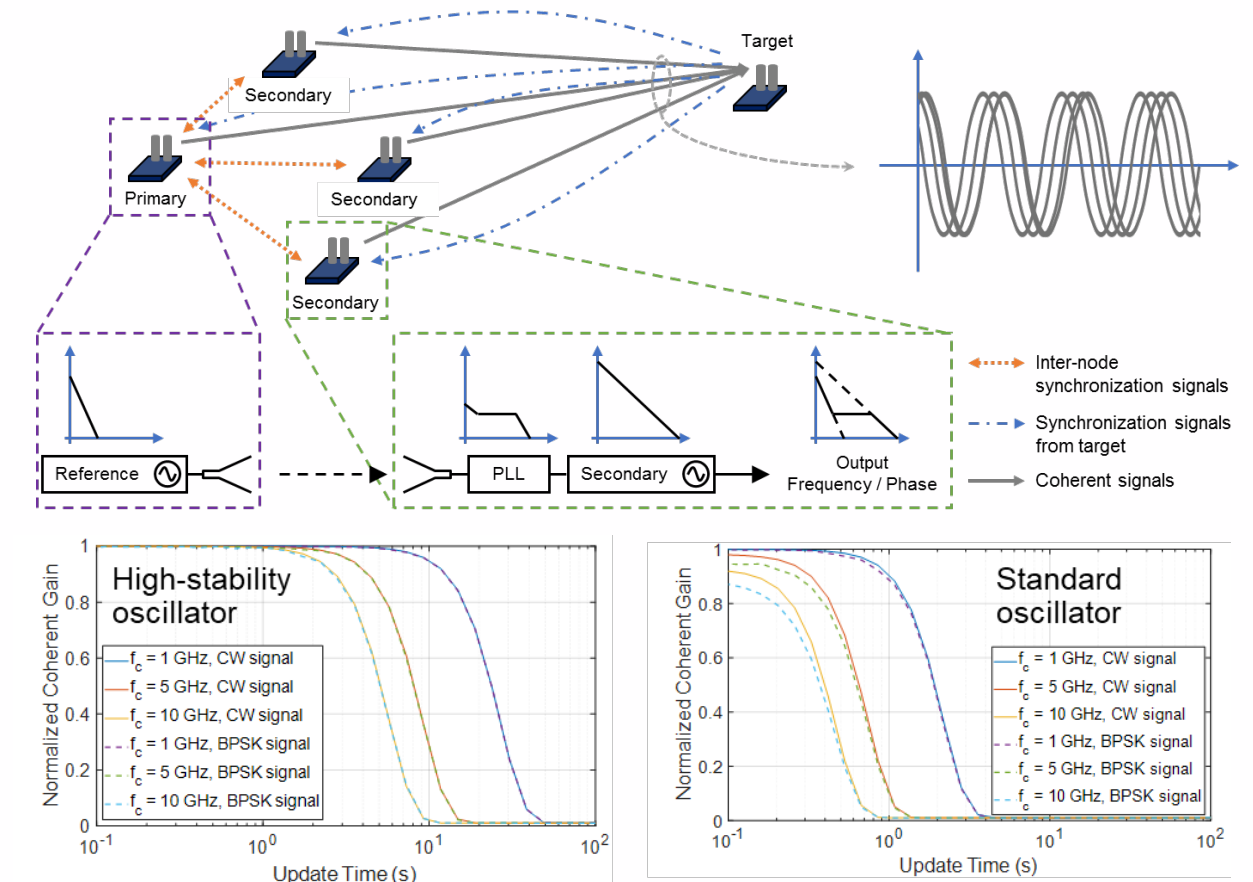
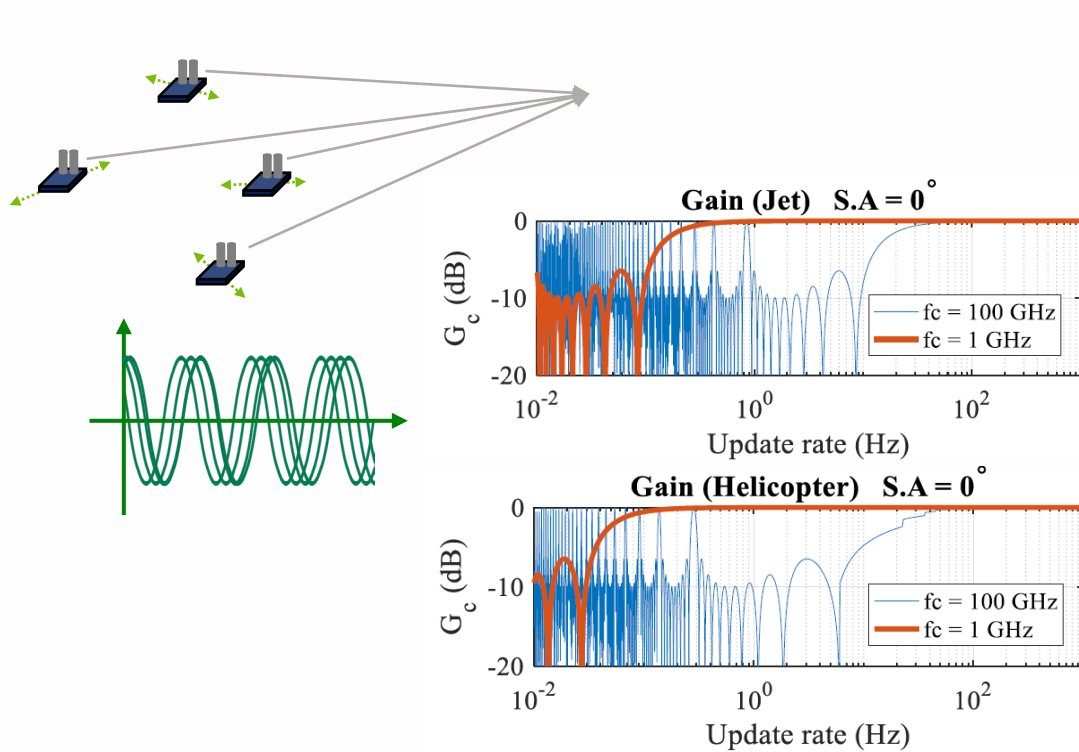


Phase error:  $18^\circ$



# System Impacts on Phase Errors

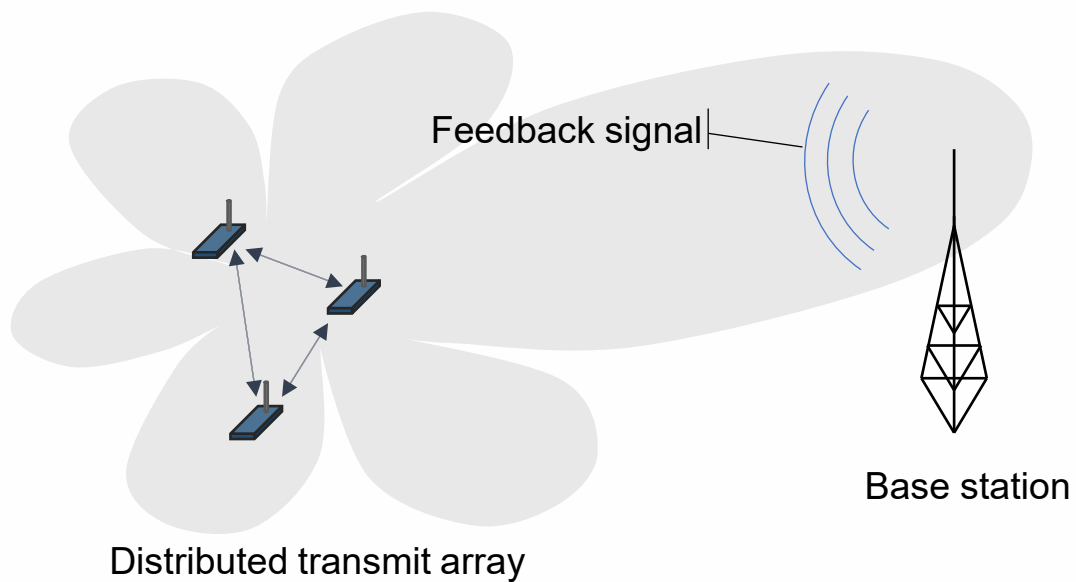
- Multiple system aspects impact beamforming performance
  - E.g.: phase noise, vibration, Doppler, system phases
- Some can be calibrated or minimized (system phase delays, Doppler)



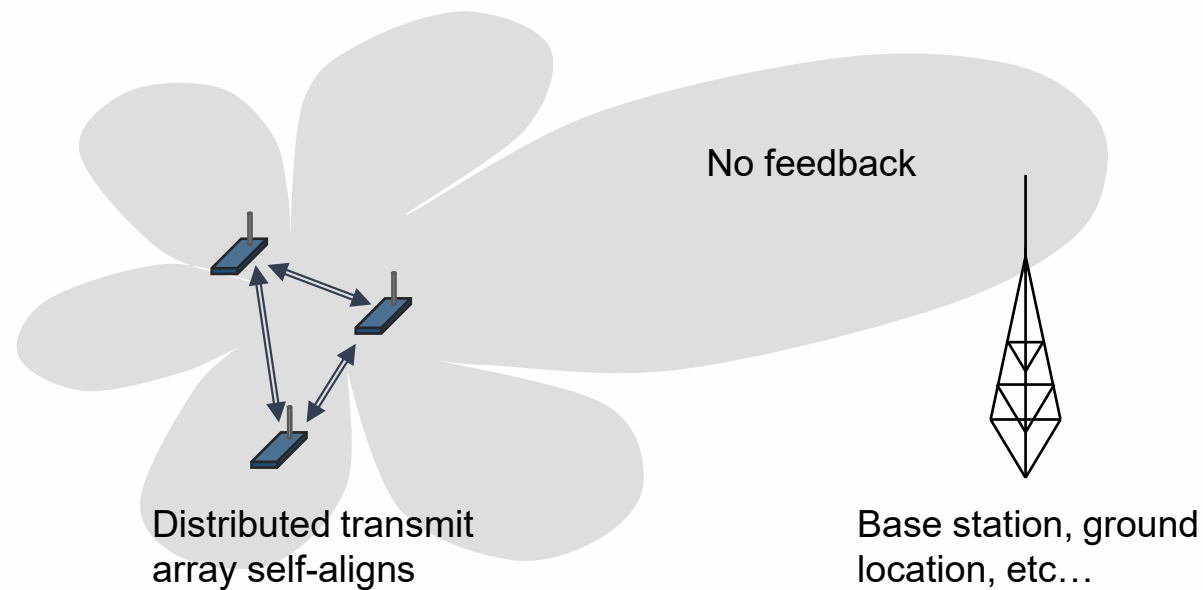
# Coordination Approaches



## Closed-Loop



## Open-Loop





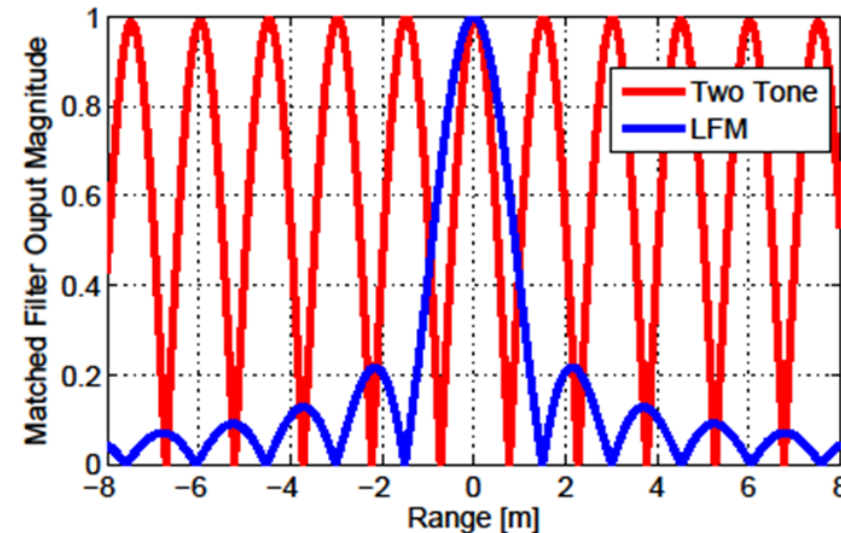
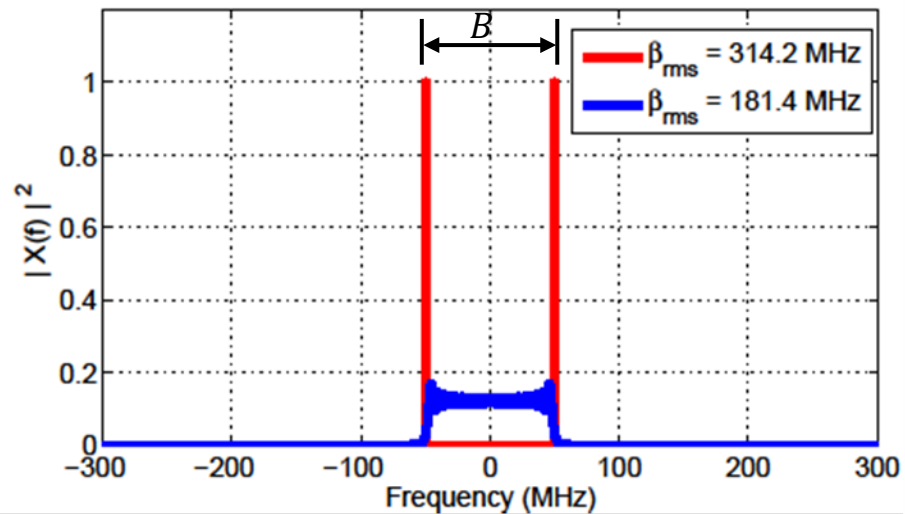
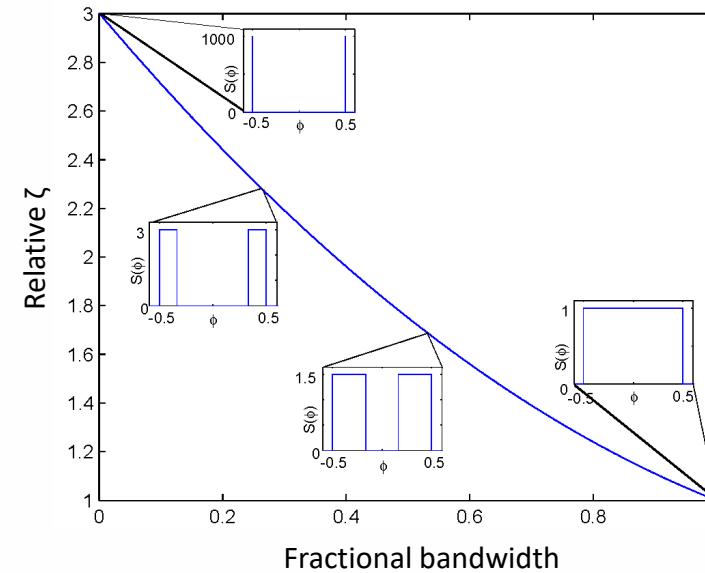
# Optimal Range Estimation

Estimation accuracy

$$\text{var}(\hat{\tau} - \tau) \geq \frac{N_o}{2|\alpha|^2 \zeta_f^2}$$

Mean-square bandwidth

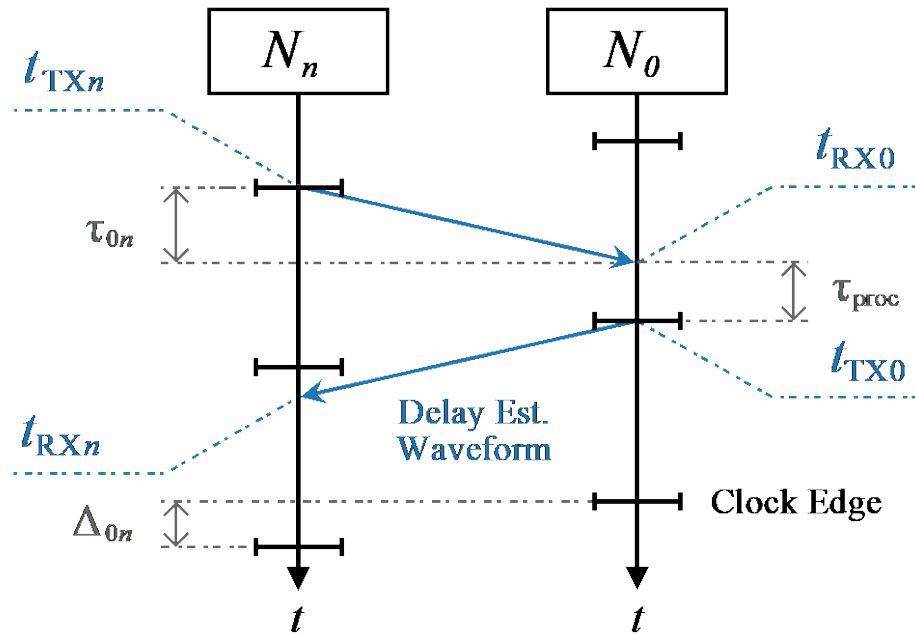
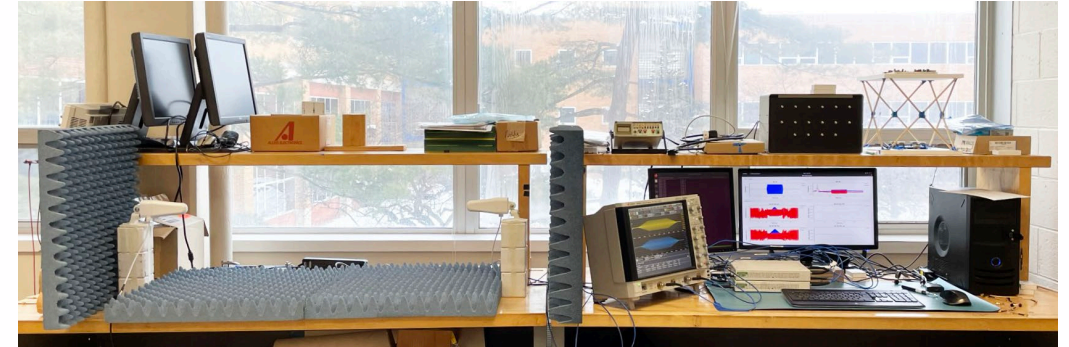
$$\zeta_f^2 = \int (2\pi f)^2 |G(f)|^2 df$$



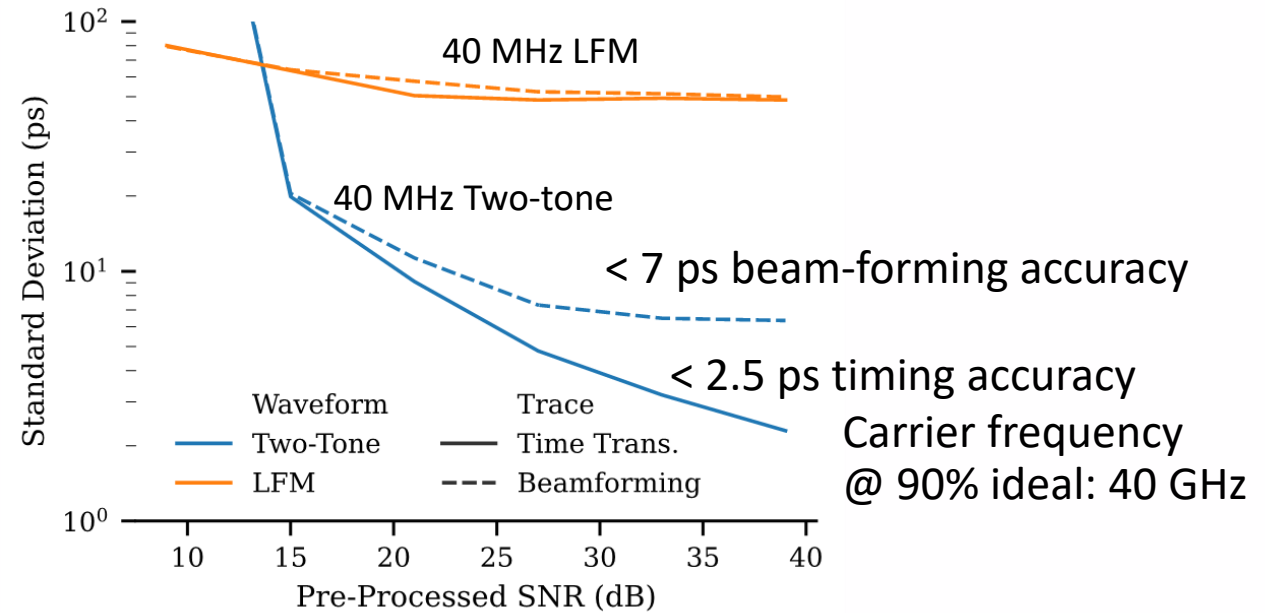


# Time Synchronization

Accurate delay estimation supports picosecond-level wireless time synchronization



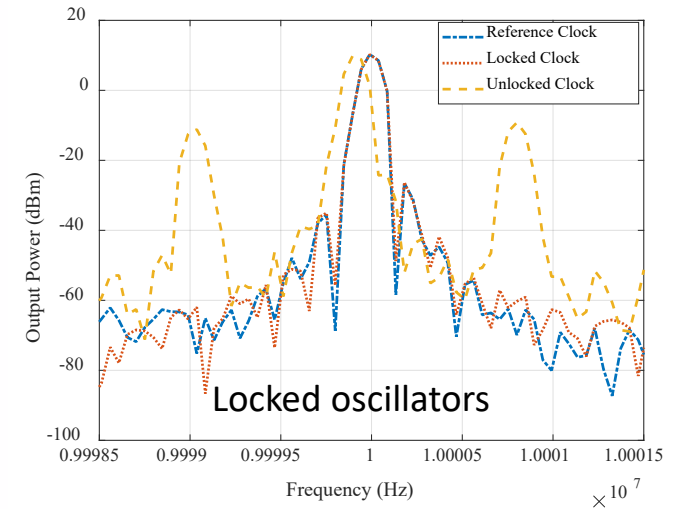
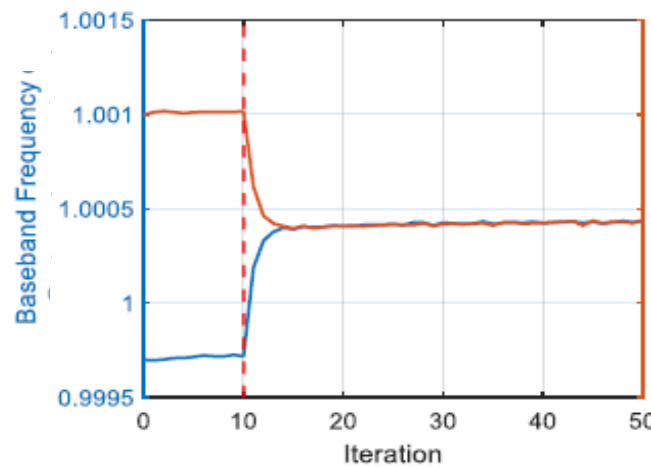
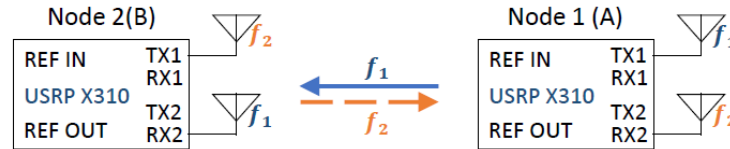
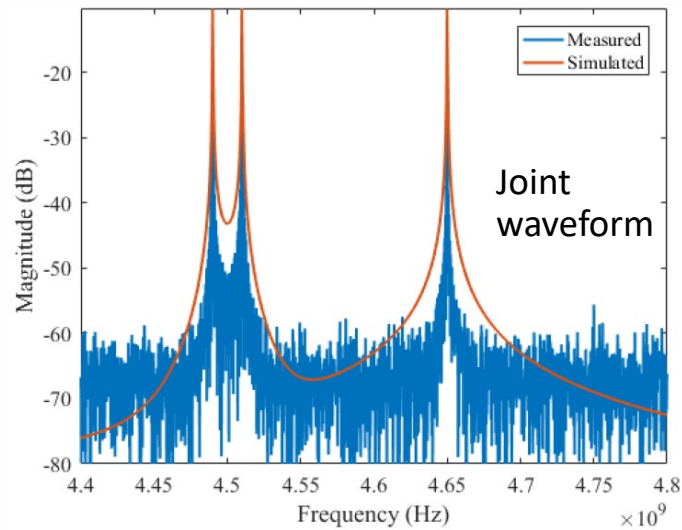
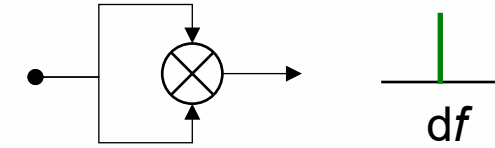
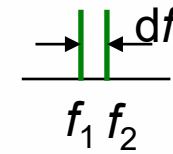
$$\Delta_{0n} = \frac{(t_{RX0} - t_{TXn}) - (t_{RXn} - t_{TX0})}{2}$$





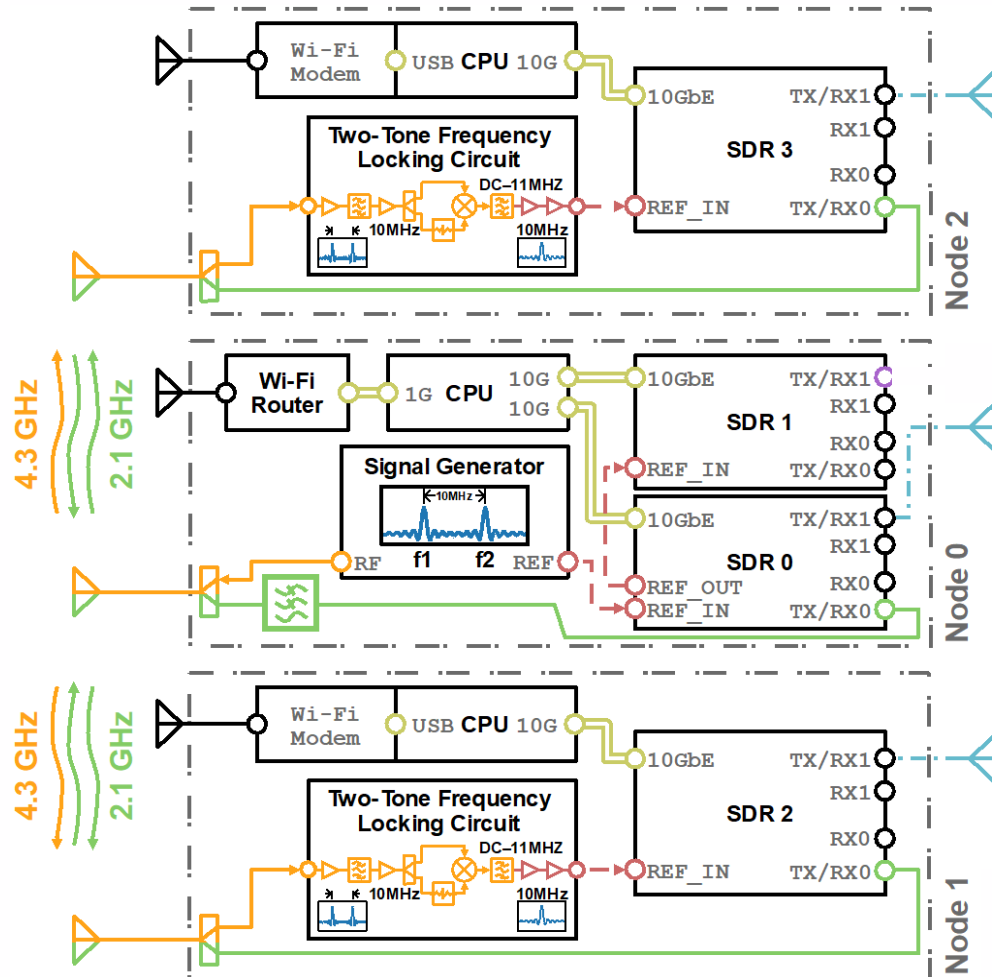
# Frequency Syntonization

Spectrally sparse waveforms support additional coordination functions, including frequency transfer



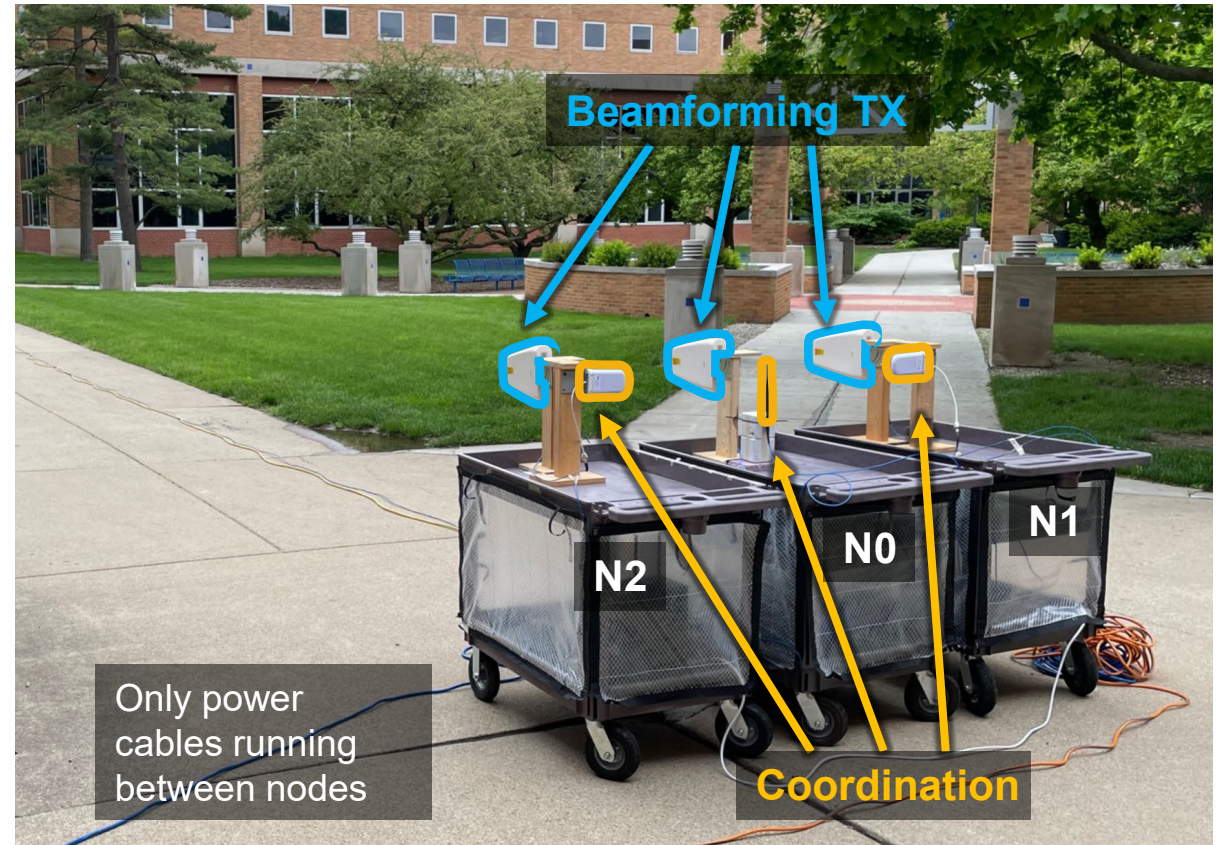


# Experiments – Typical Configuration



## Legend

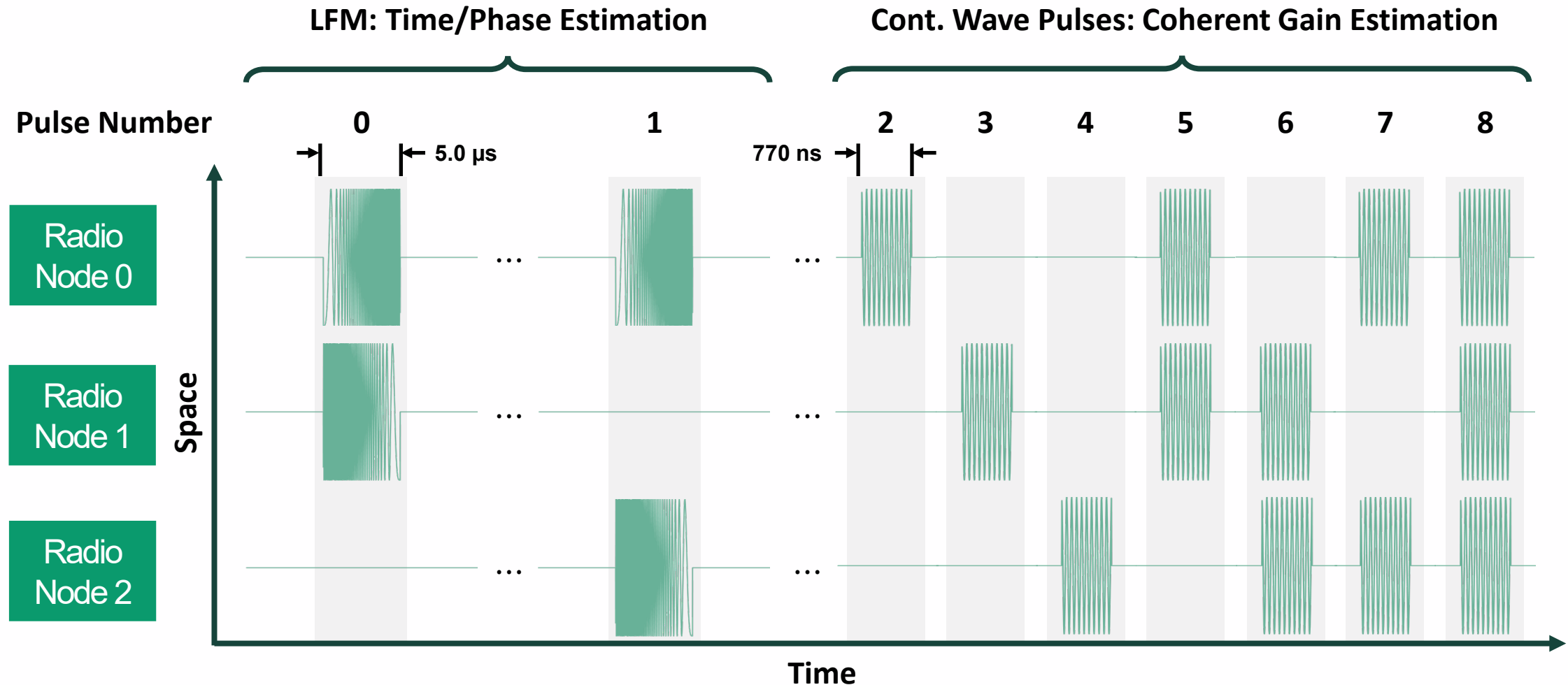
- Time Transfer Waveform
- Frequency Transfer Waveform
- - - 10 MHz Freq. Reference
- Data
- - - Beamforming Waveforms





# Beamforming/Beamsteering Evaluation

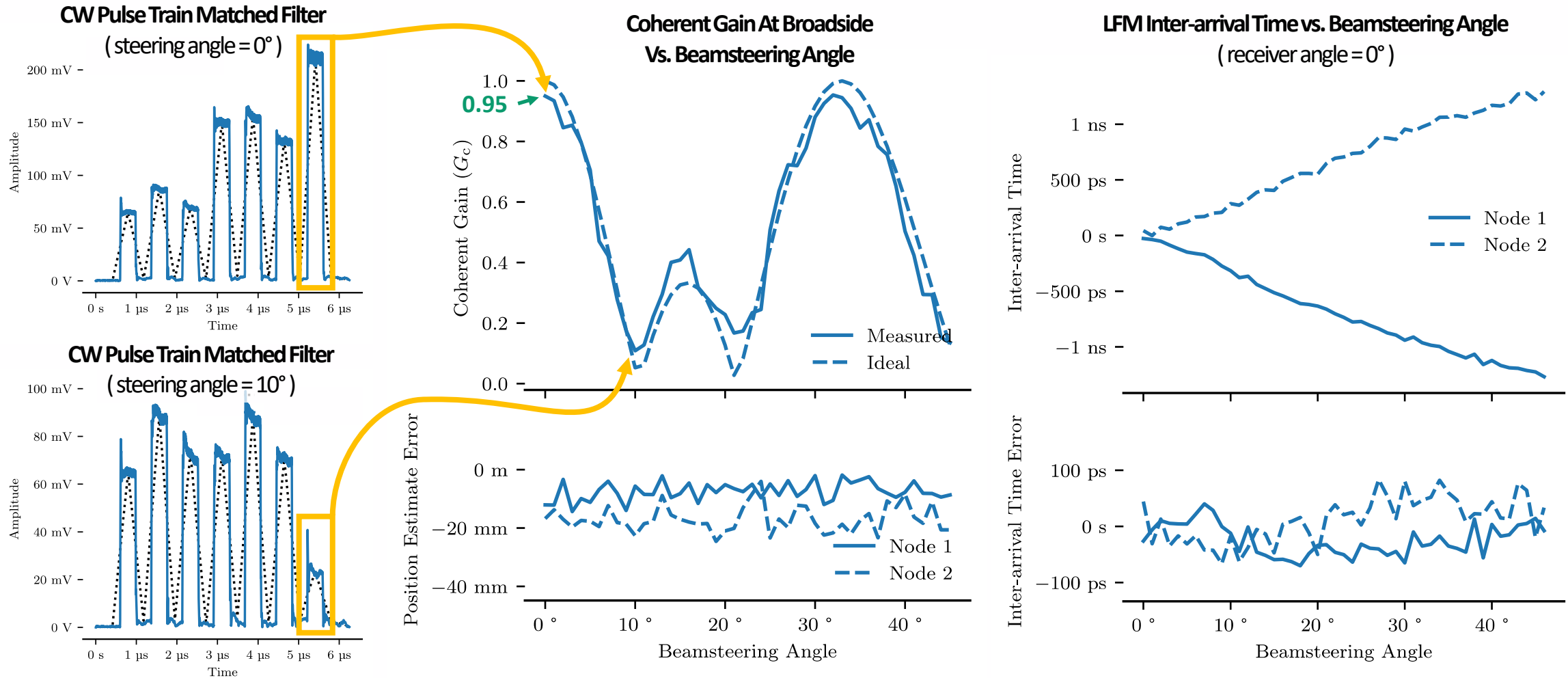
- Each node transmitted orthogonal LFM's followed by continuous wave pulse train



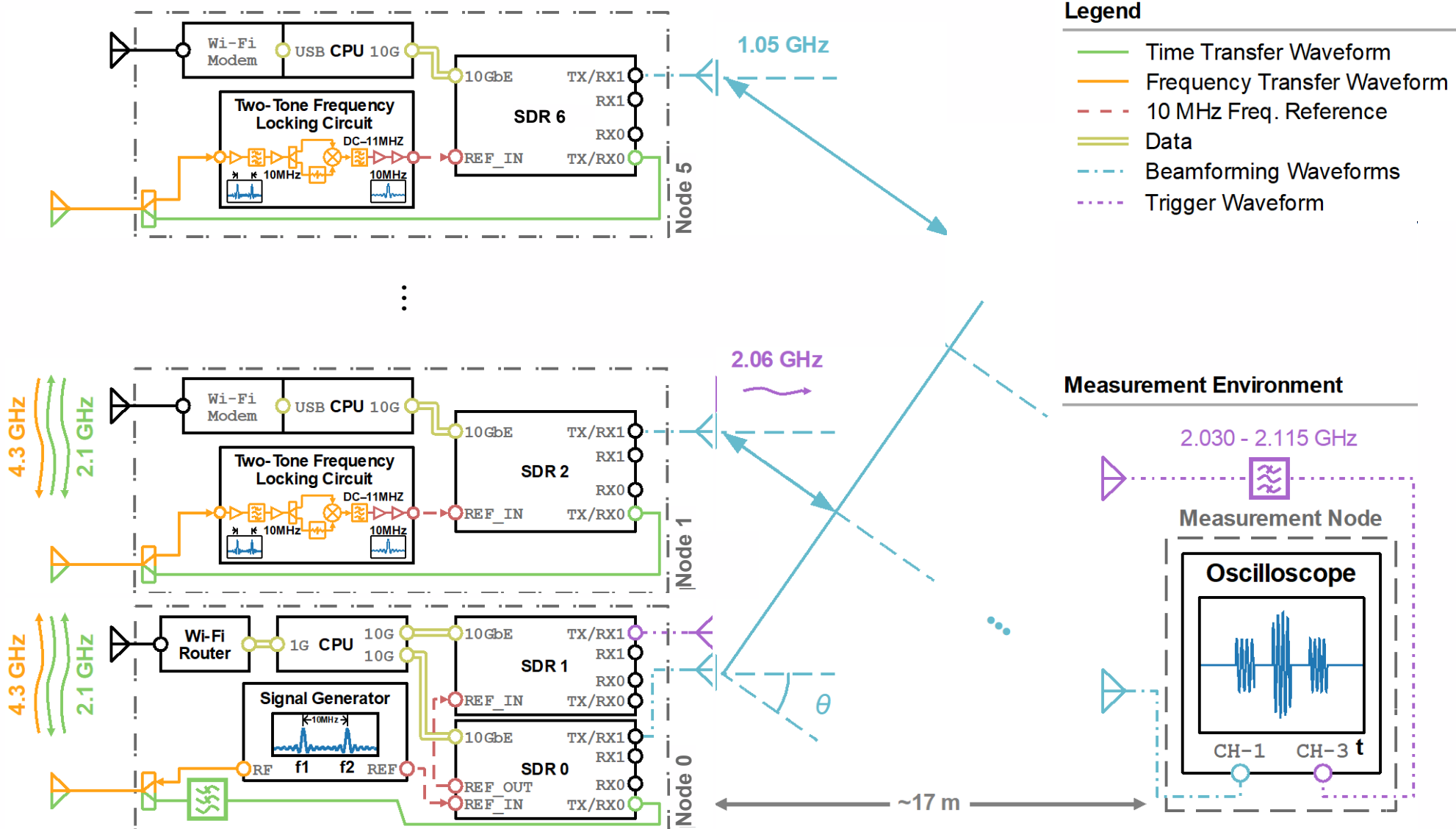
# Beamforming/Beamsteering Evaluation



Beamsteering measurements at a static receiver



# Six-node Beamforming with Decentralized Time Synchronization



# Six-node Beamforming with Decentralized Time Synchronization

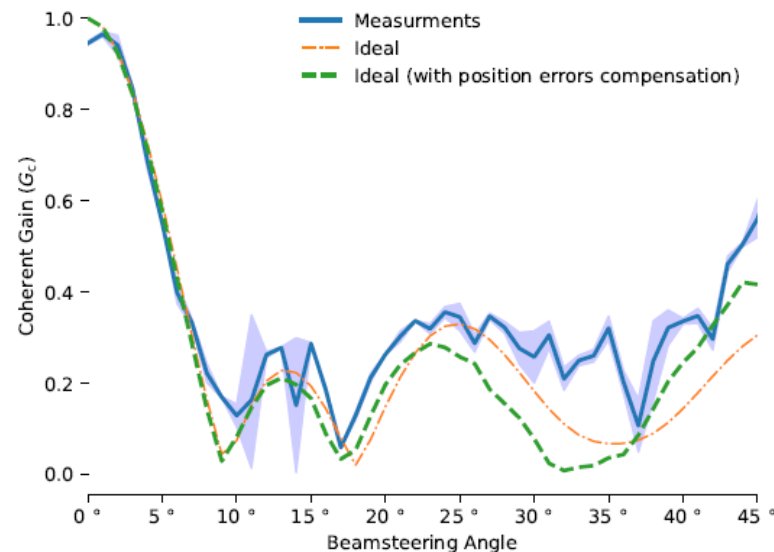


# Six-node Beamforming with Decentralized Time Synchronization

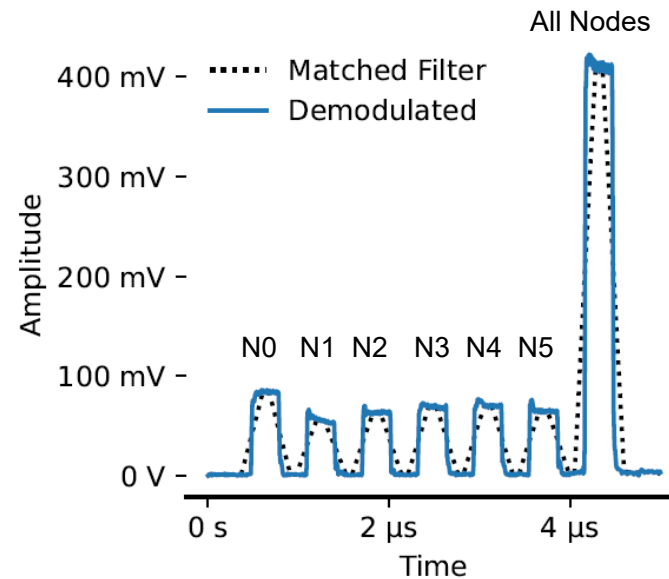


- Receiver held static; beam steered from  $0^\circ$  to  $45^\circ$
- Decentralized time synchronization; centralized analog frequency syntonization
- Average coherent gain  $> 98\%$  at  $f_c = 1.05$  GHz

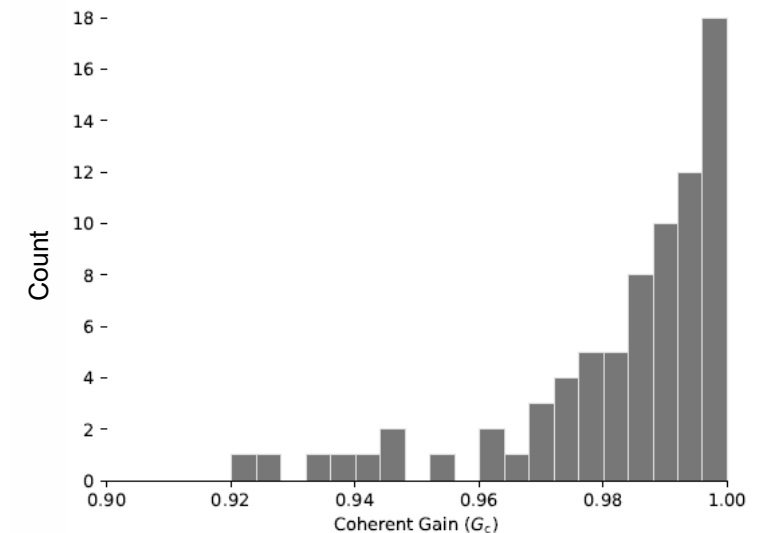
Array pattern while steering



Single pulse (fast time)



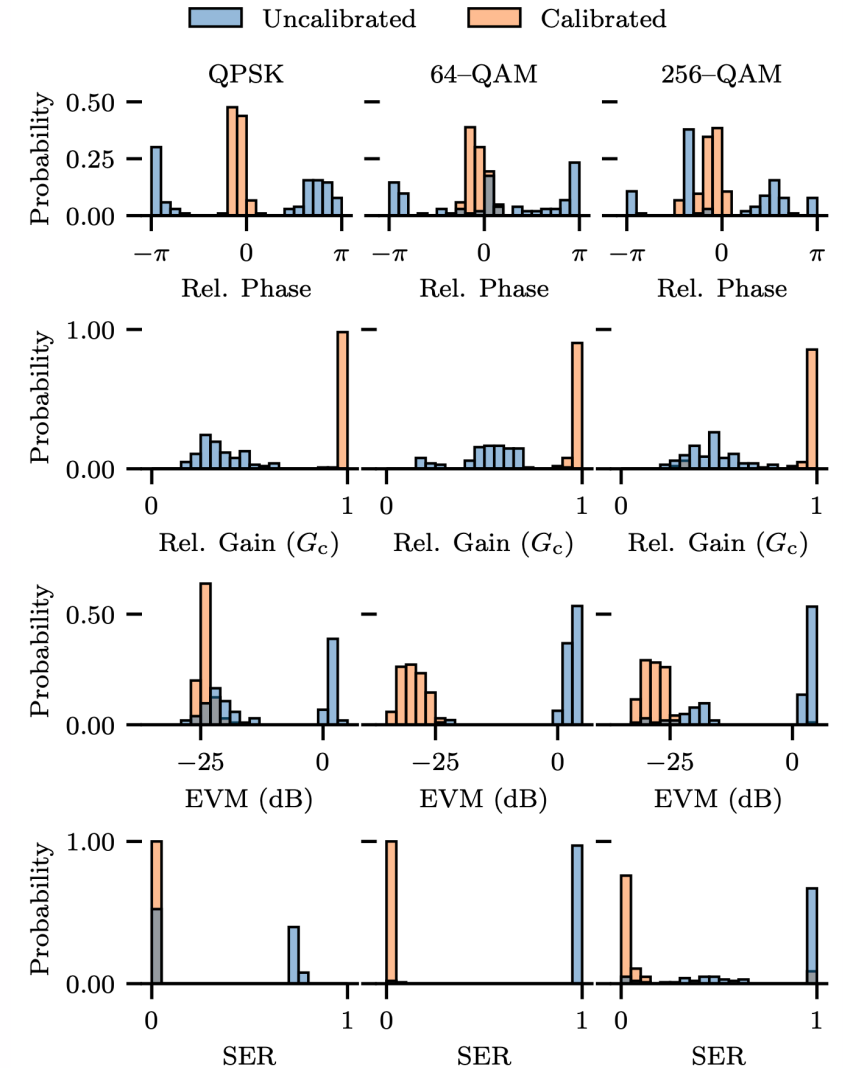
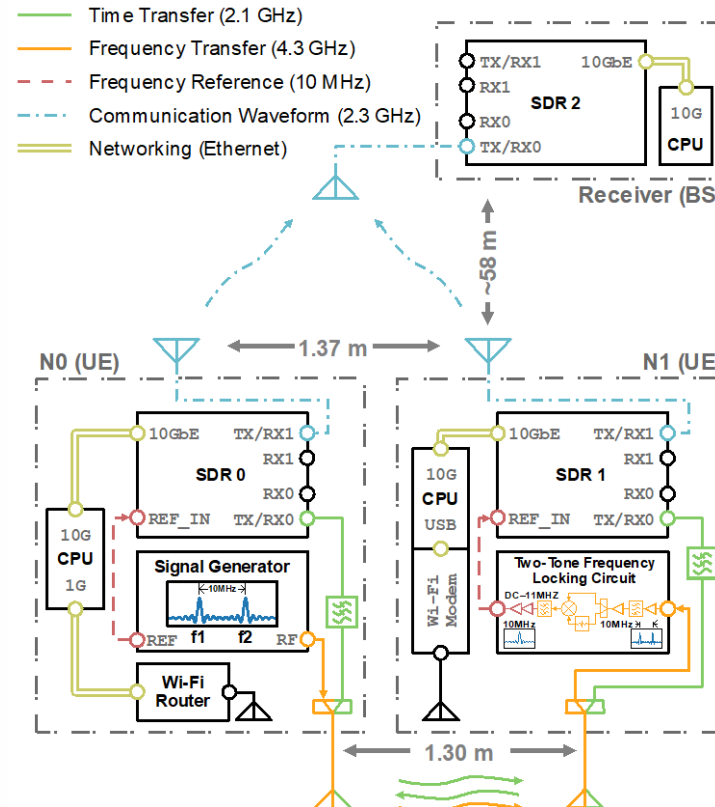
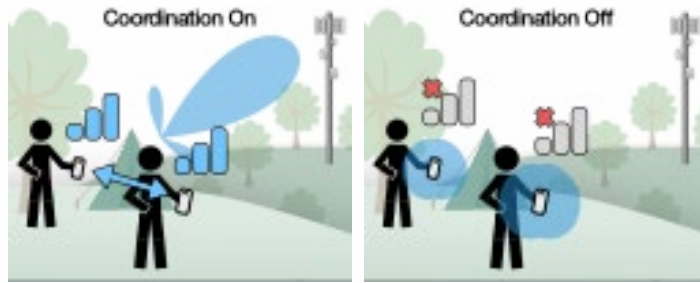
Histogram of coherent gain



# Coherent Distributed Communications



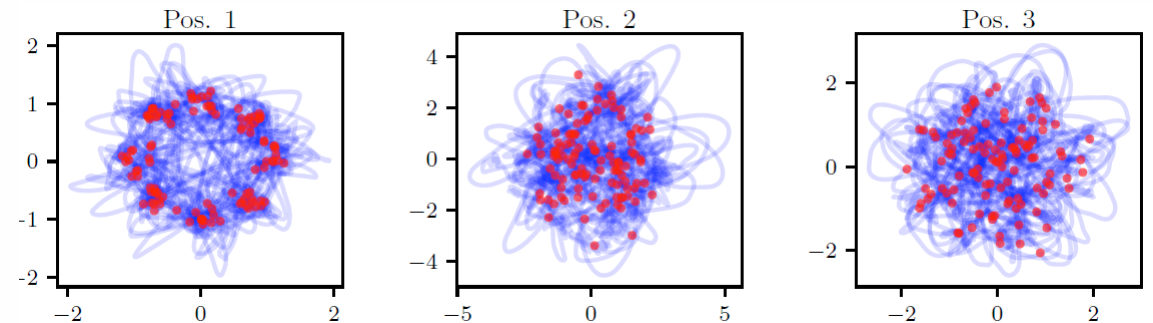
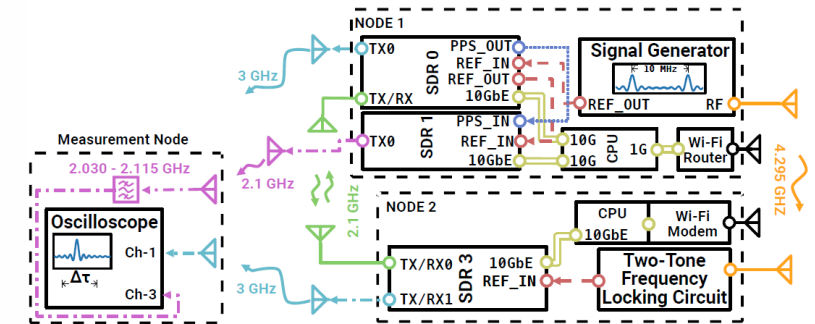
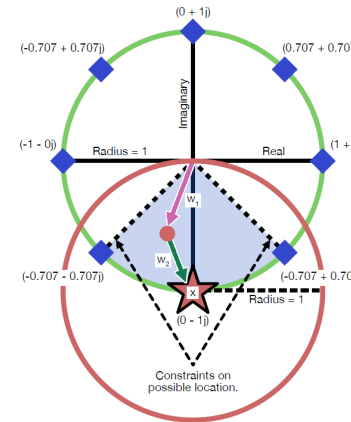
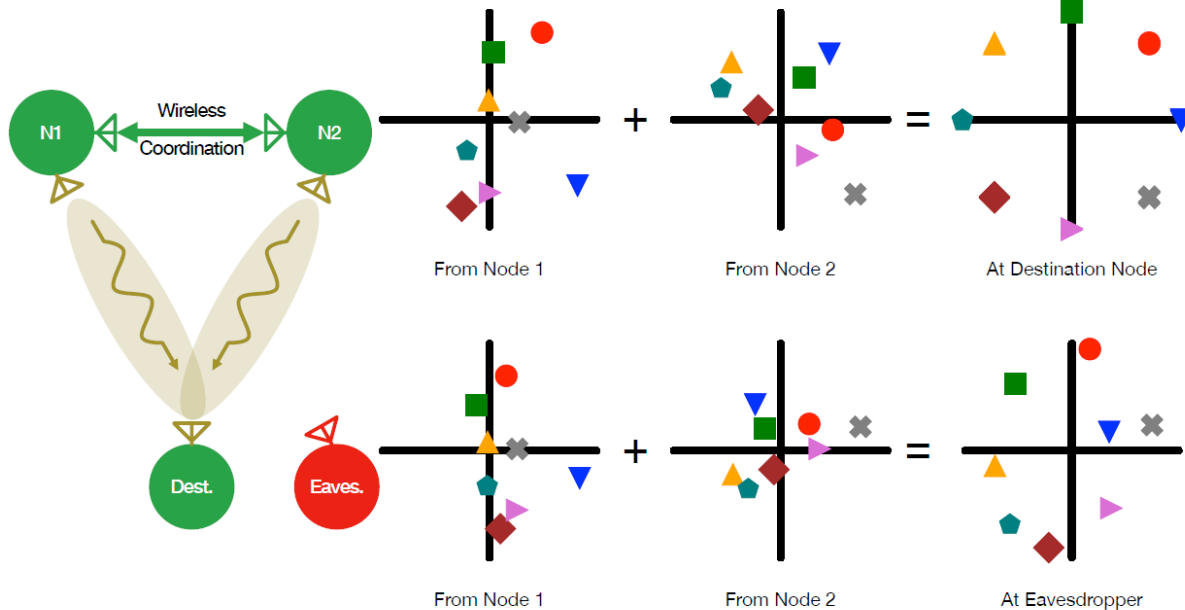
- Demonstrated initial proof of concept of a distributed communication system transmitting QAM symbols
- Demodulated on a single software-defined radio receiver



# Distributed Communications for Wireless Security



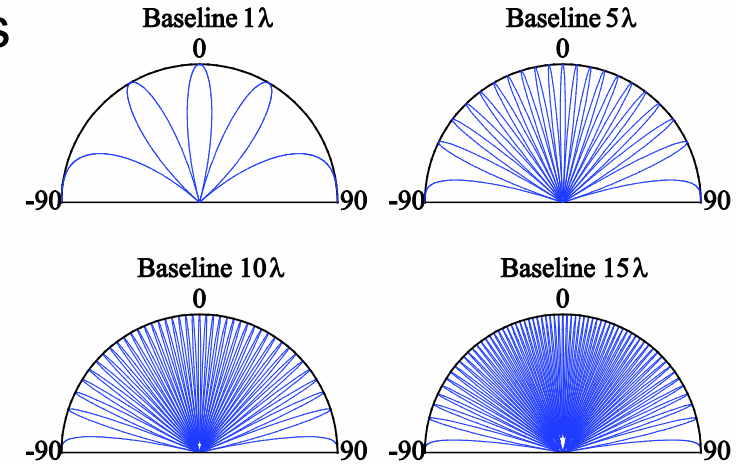
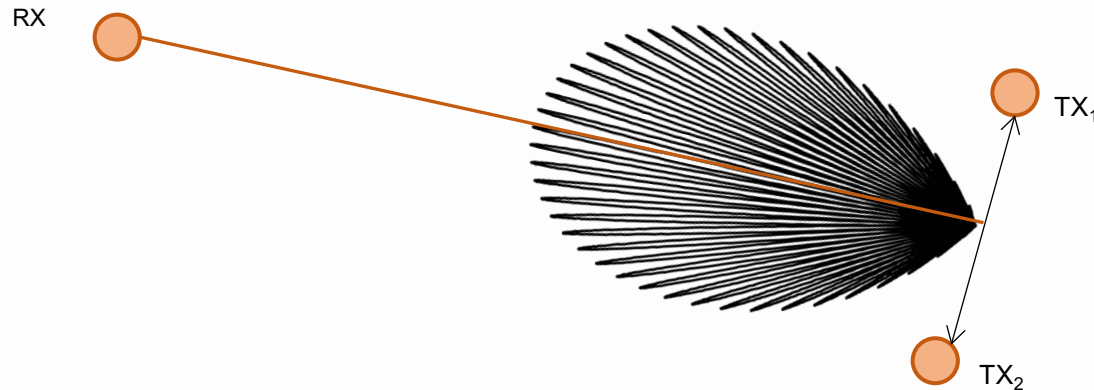
- Coherent transmission of spatially decomposed signals
- Coherent reception at desired receiver, random constellations at other angle



# Grating Lobes

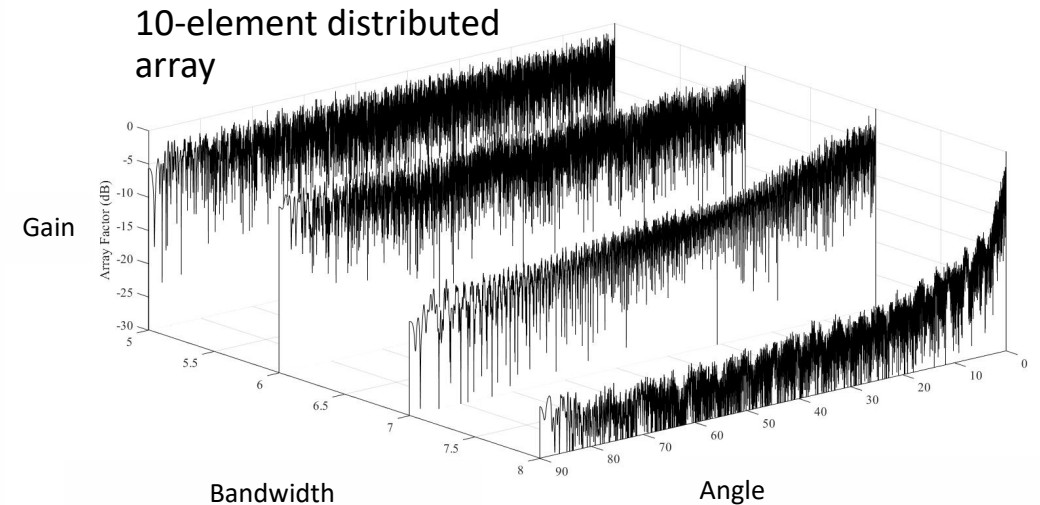


Spatial ambiguities are inherent in sparse antenna arrays



Typical approach: mitigation, e.g., via bandwidth

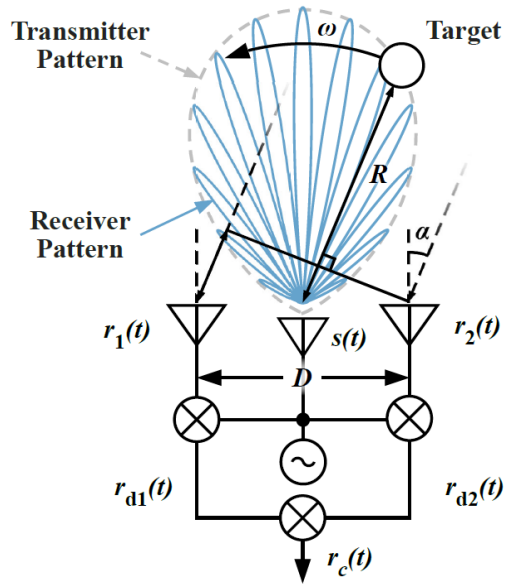
- Typically very wide bandwidths are needed
- Often reduces grating lobe energy far from mainbeam area, but can leave grating lobes near the mainbeam largely unaffected



# Grating Lobes – Sensing



Using grating lobes for new radar measurements



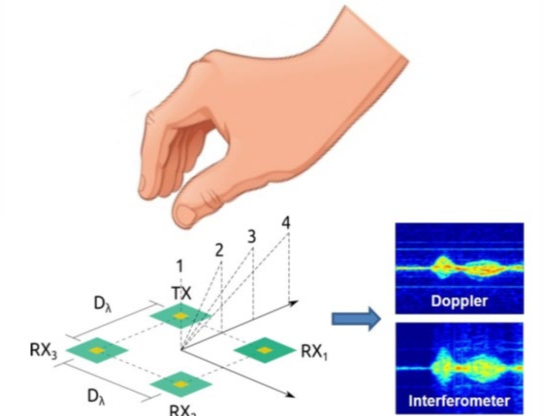
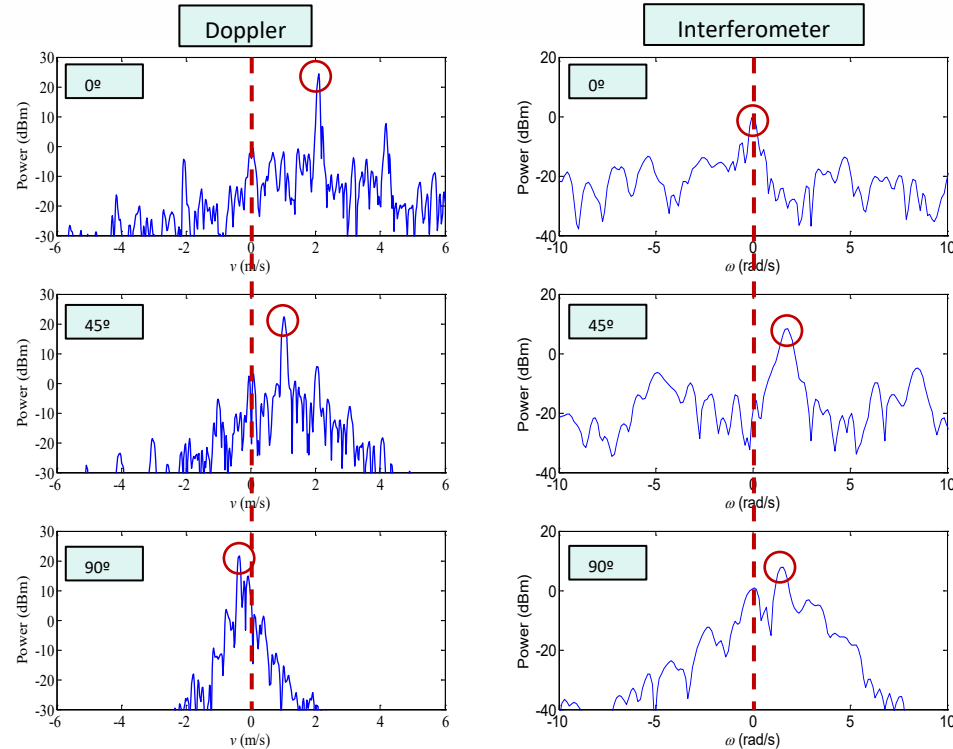
Interferometer  
Frequency shift

$$f_s = \frac{\omega D}{\lambda_c}$$

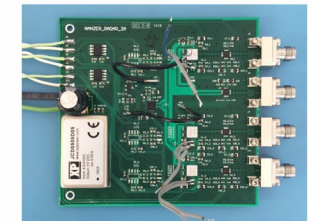
Doppler  
frequency shift

$$f_D = \frac{2v_r}{\lambda_c}$$

Joint Doppler/interferometer measurements



40 GHz interferometric radar



Gesture classification

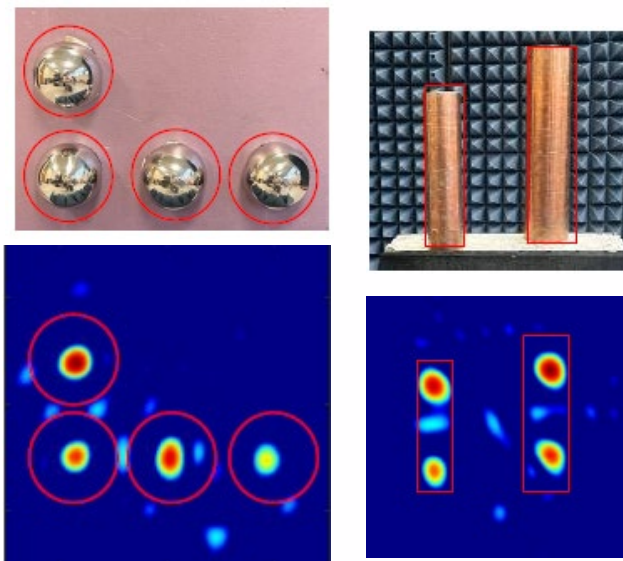
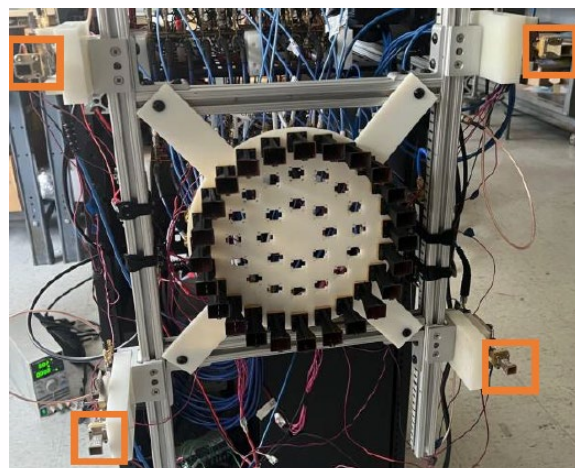
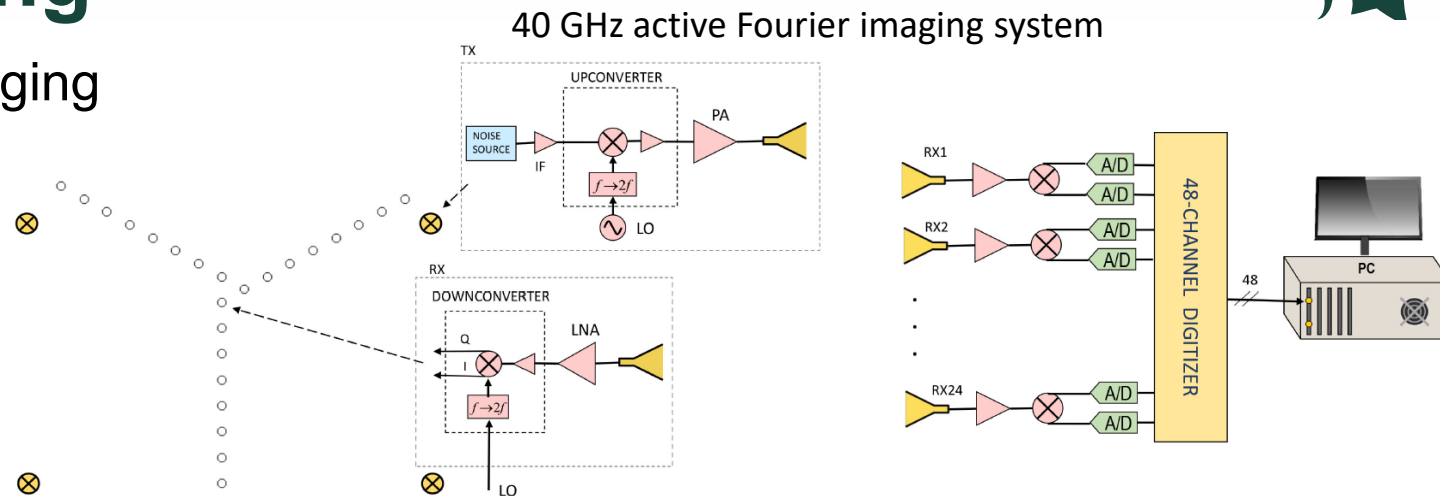
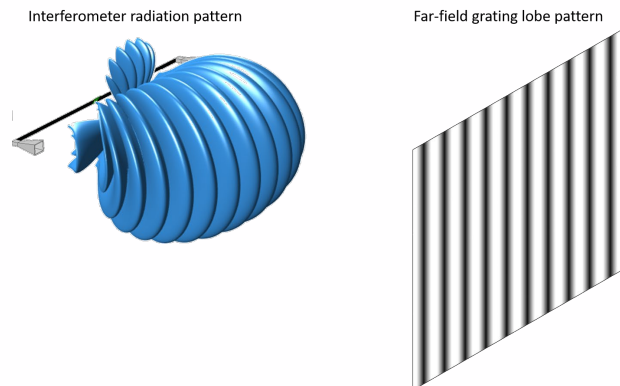
0	1	0	0	0	0
1	0	1	0	0	0
2	0	0	1	0	0
3	0.067	0	0	0.93	0
4	0	0	0	0	1
	0	1	2	3	4

IEEE TMTT 58 (12) 2010  
IEEE TAP 60 (11) 2012  
IEEE TAP 62 (3) 2014

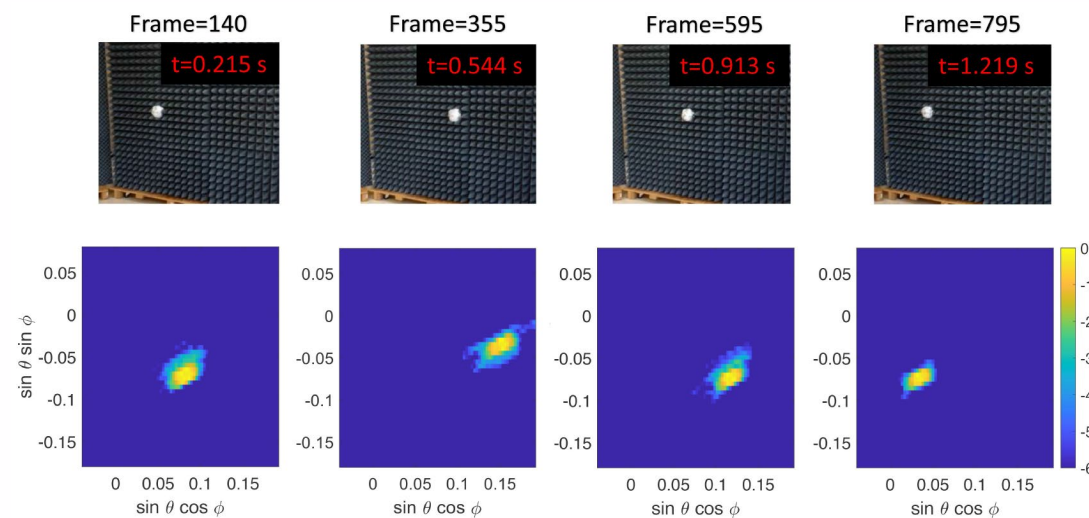
IEEE MWCL 30 (3) 2020  
IEEE TMTT 69 (1) 2021  
IEEE MWCL 31 (8) 2021

# Grating Lobes – Sensing

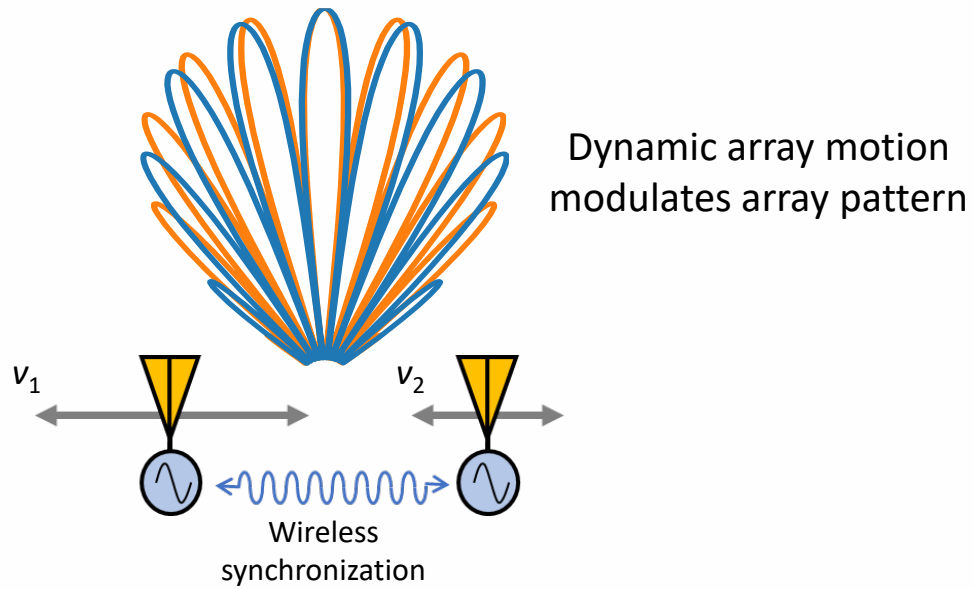
Using grating lobes for fast Fourier imaging



## High-speed image reconstruction



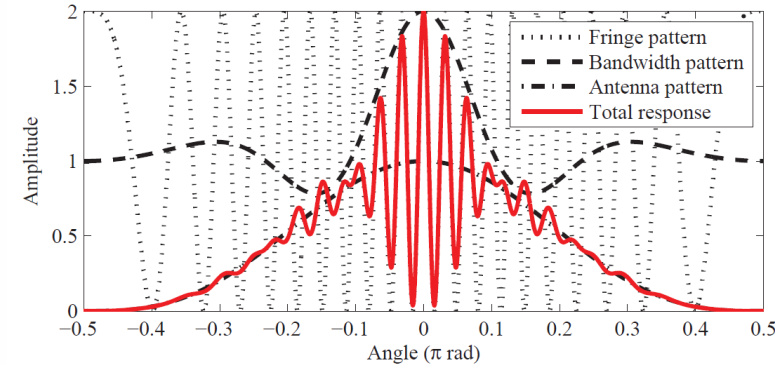
# Mitigation of Grating Lobes Using Array Dynamics



Combining spatial motion and frequency bandwidth

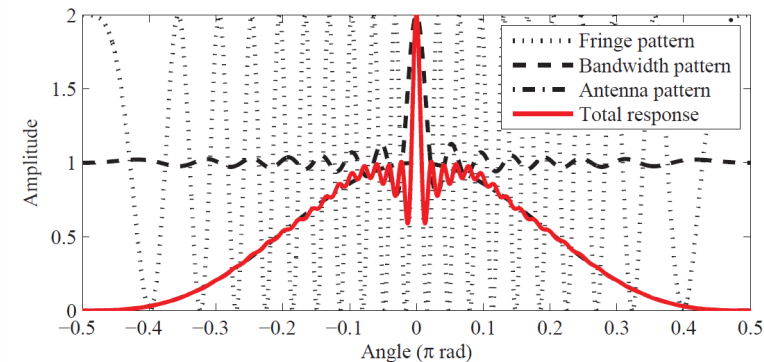
$$s_r(t, \theta) = \chi(t)A(\theta) \frac{\Delta d_\lambda}{2} [1 + e^{-j2\pi d_0 \sin\theta} \text{sinc}(\pi \Delta d_\lambda \sin\theta)]$$

$$\Delta d_\lambda = \Delta d / \Delta \lambda$$



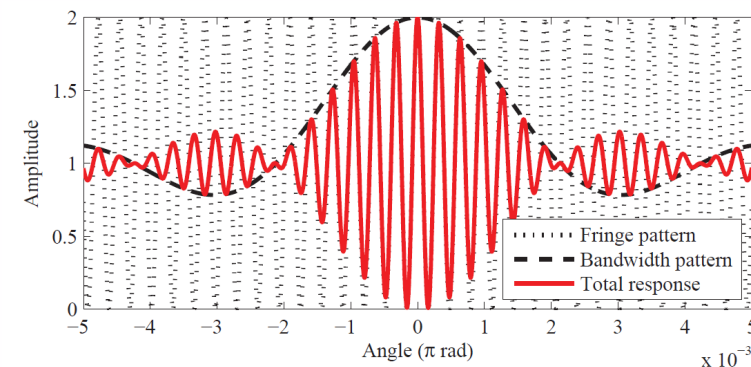
$$D = 10\lambda$$

$$\Delta d_\lambda = 3$$



$$D = 10\lambda$$

$$\Delta d_\lambda = 15$$

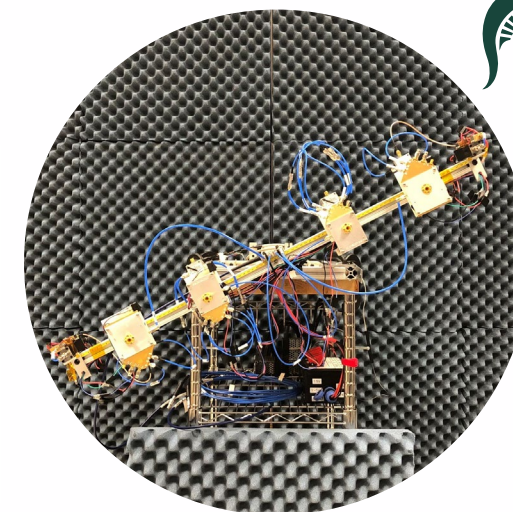


$$D = 1000\lambda$$

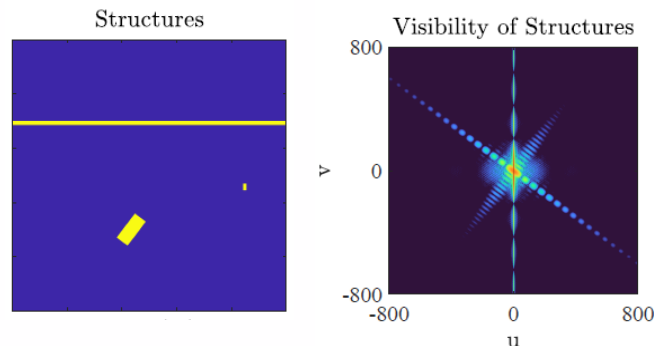
$$\Delta d_\lambda = 150$$

# Fourier Domain Sensing

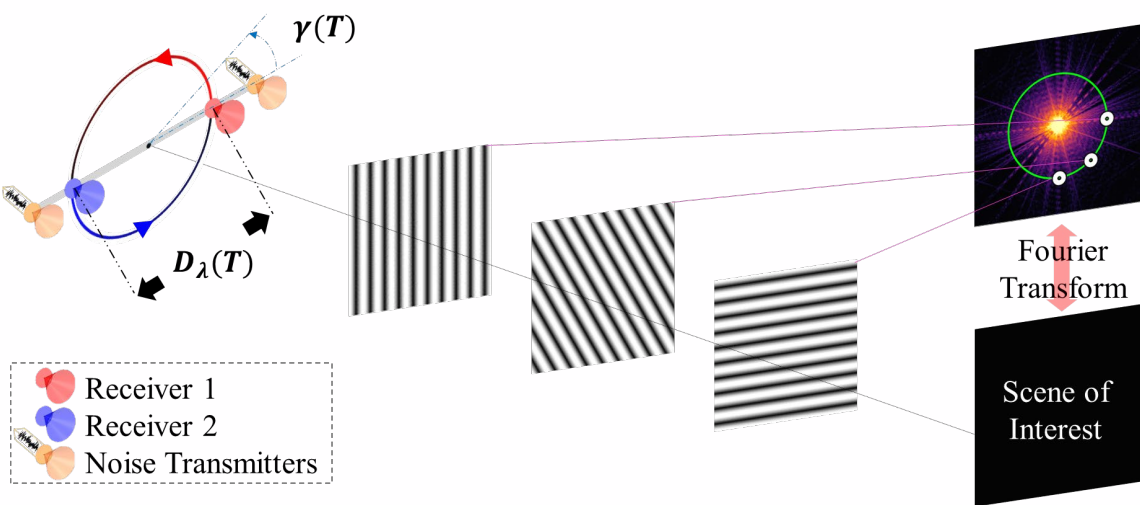
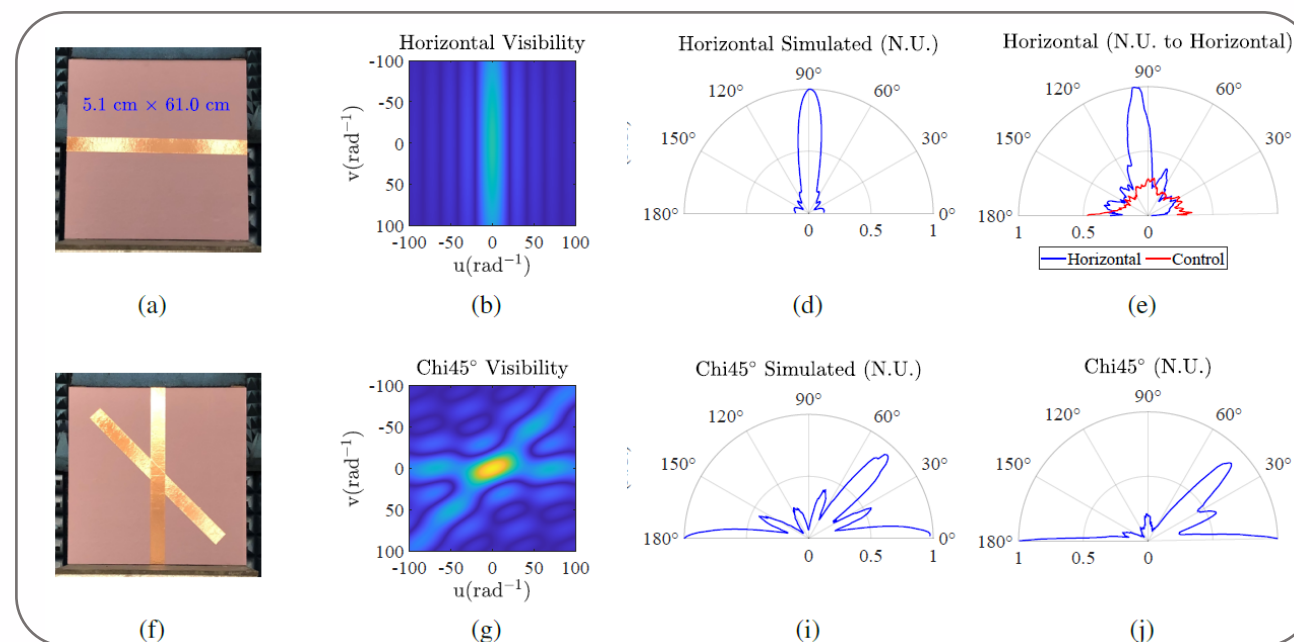
Using Fourier-domain sampling and dynamics for imageless object detection



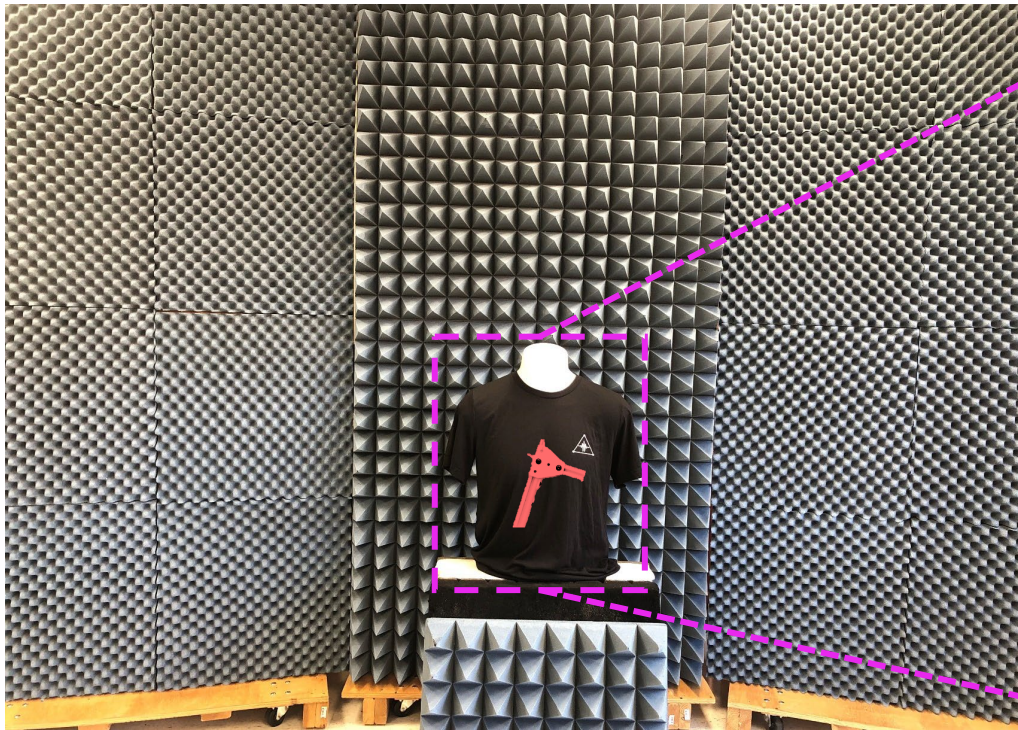
Fourier features



Fourier-domain feature detection



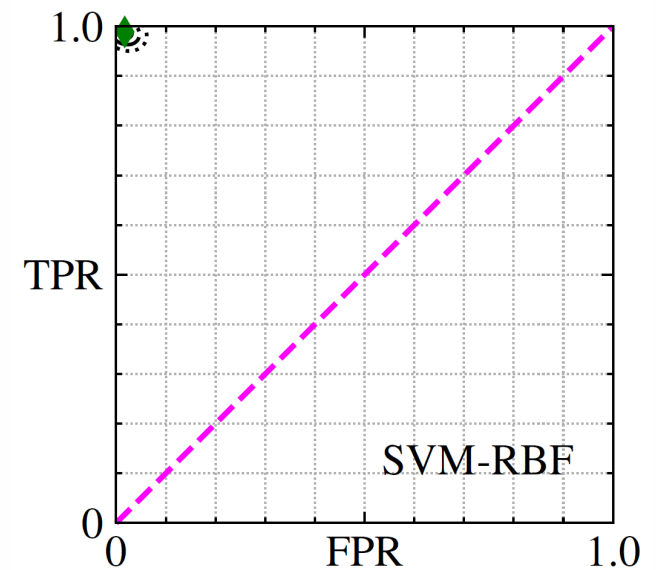
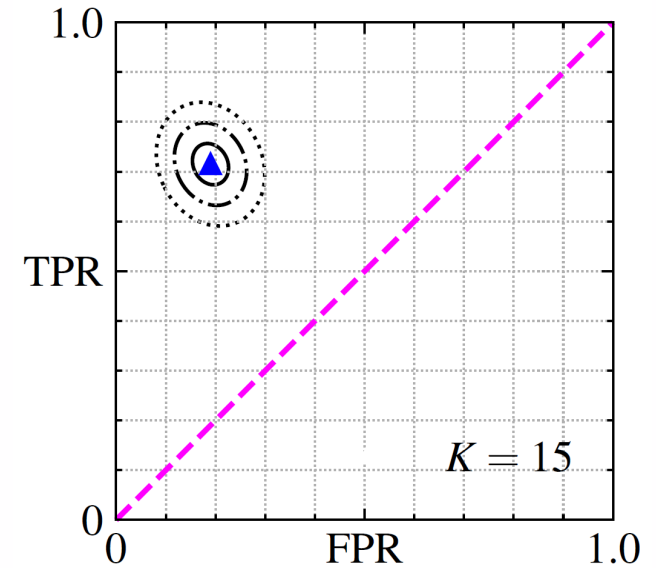
# Fourier Domain Sensing



Gs: Gun-shape



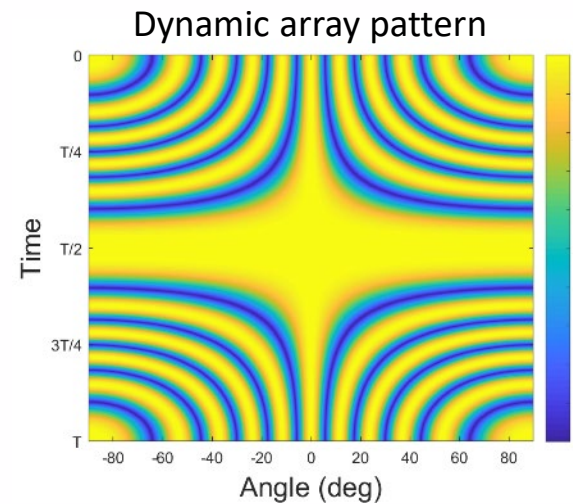
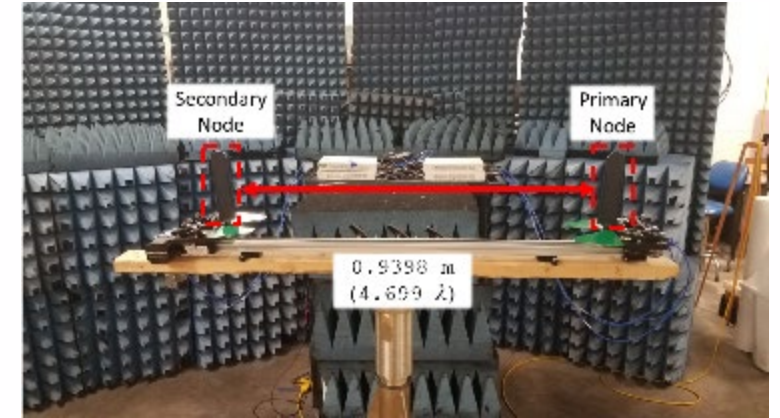
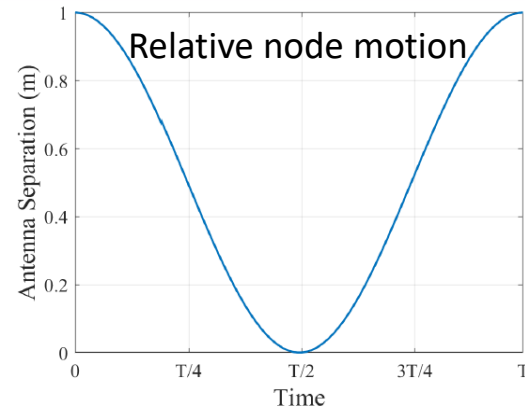
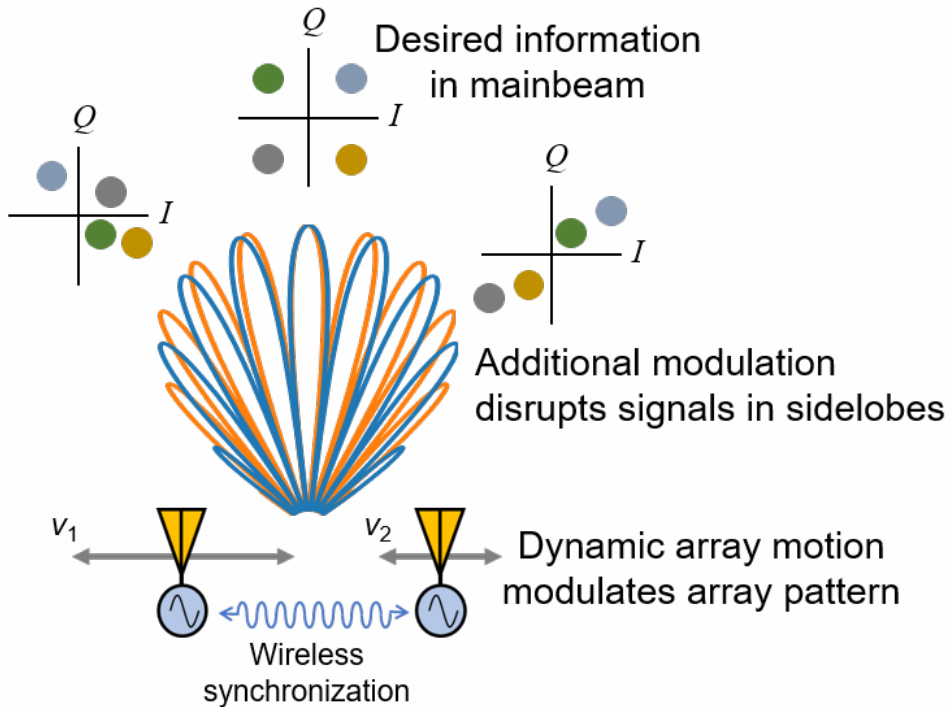
nGs: non-Gun-shape





# Directional Modulation

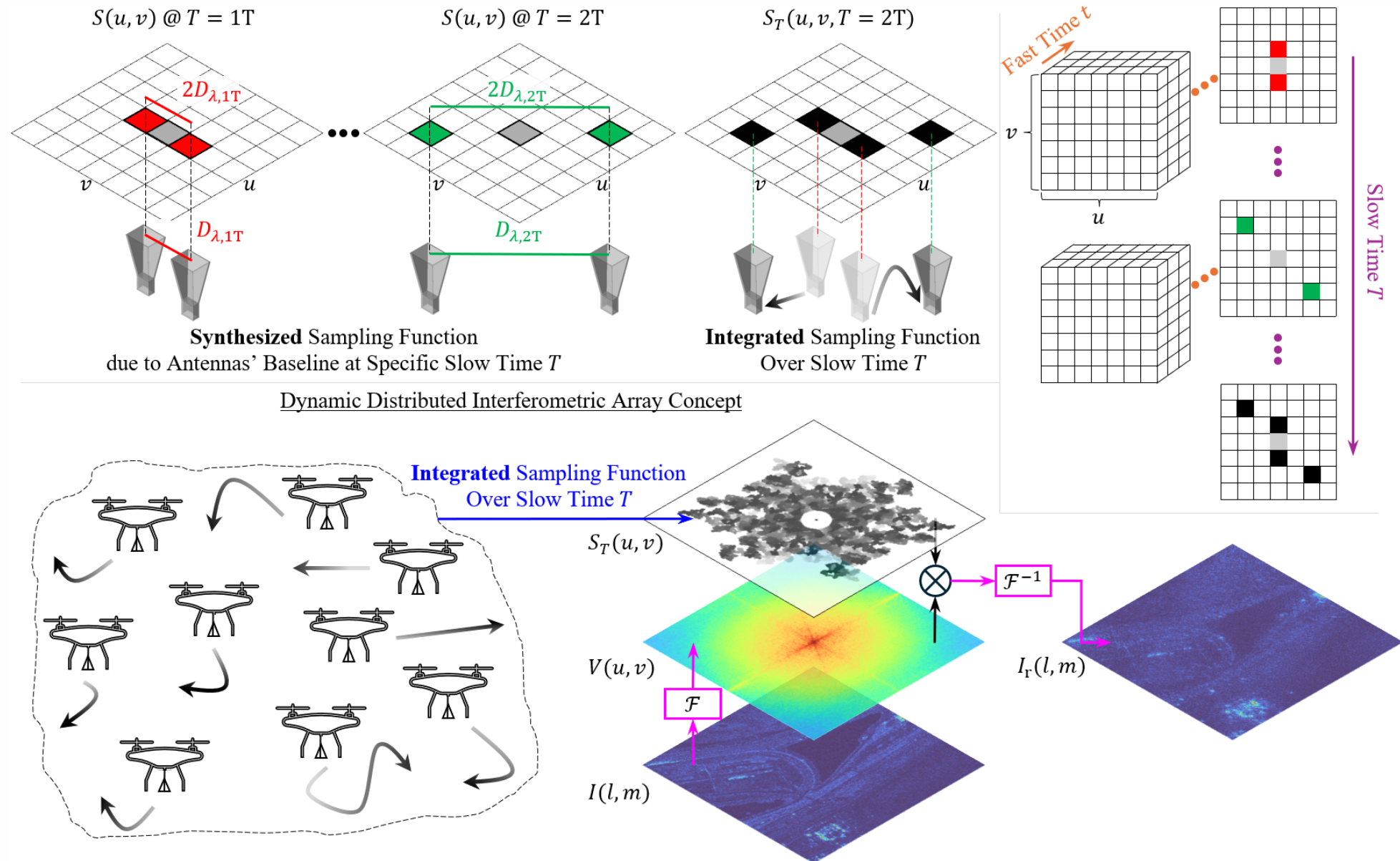
Using spatiotemporal dynamics for secure wireless



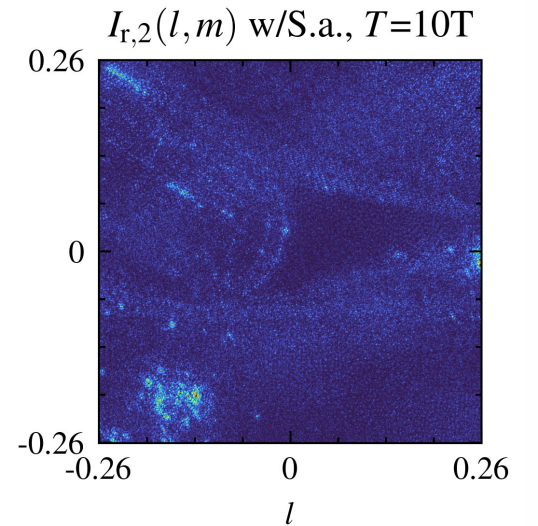
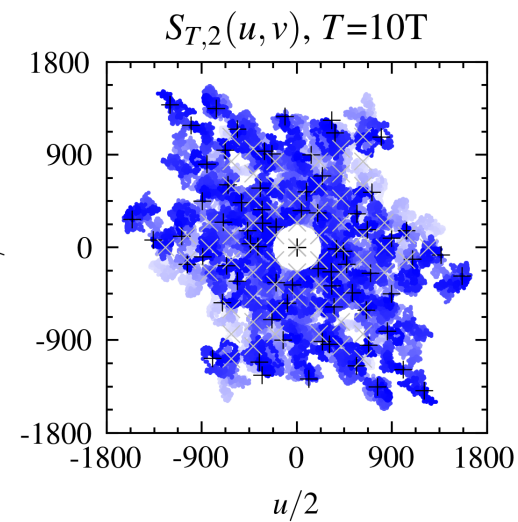
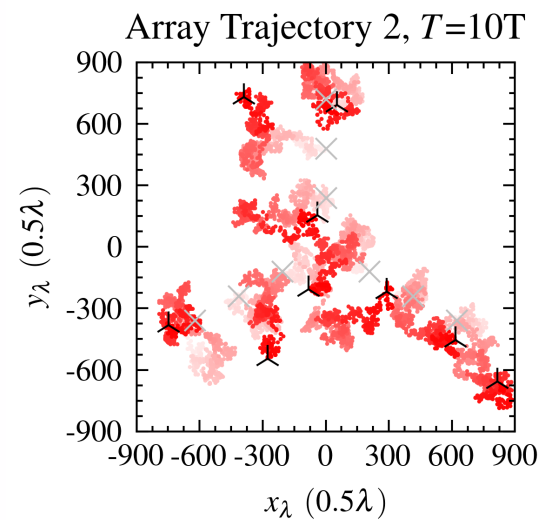
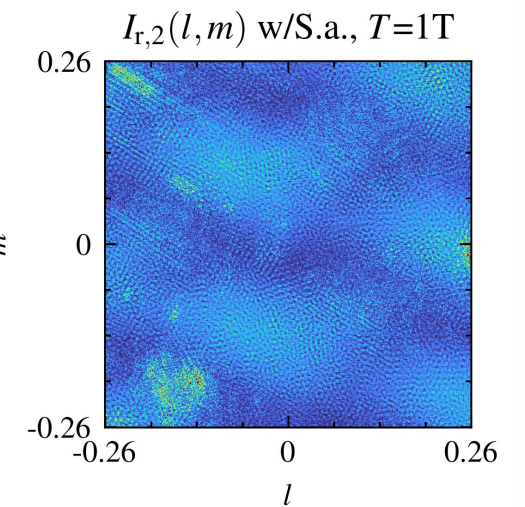
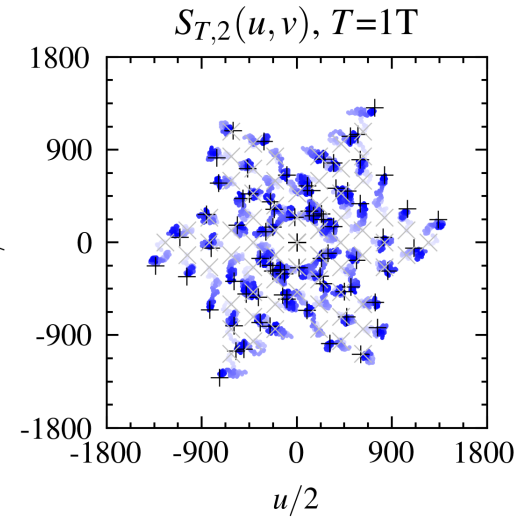
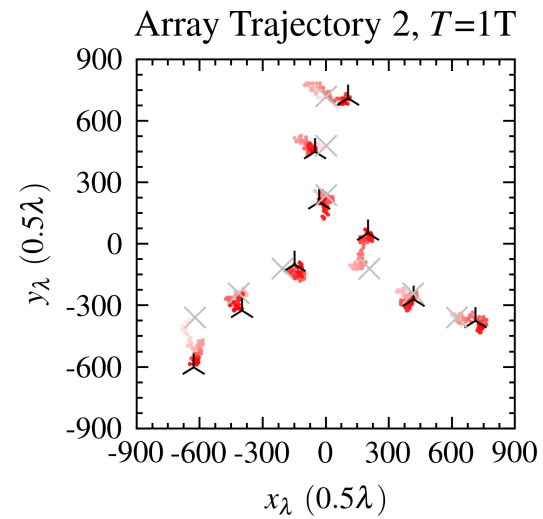
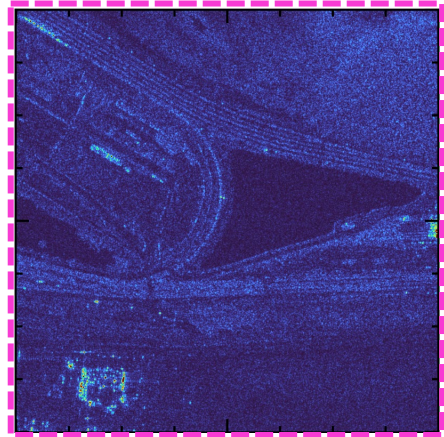
Distributed arrays: Signal gain in grating lobes reduces from  $N^2$  to  $N$



# Increased Distributed Fourier Domain Sampling



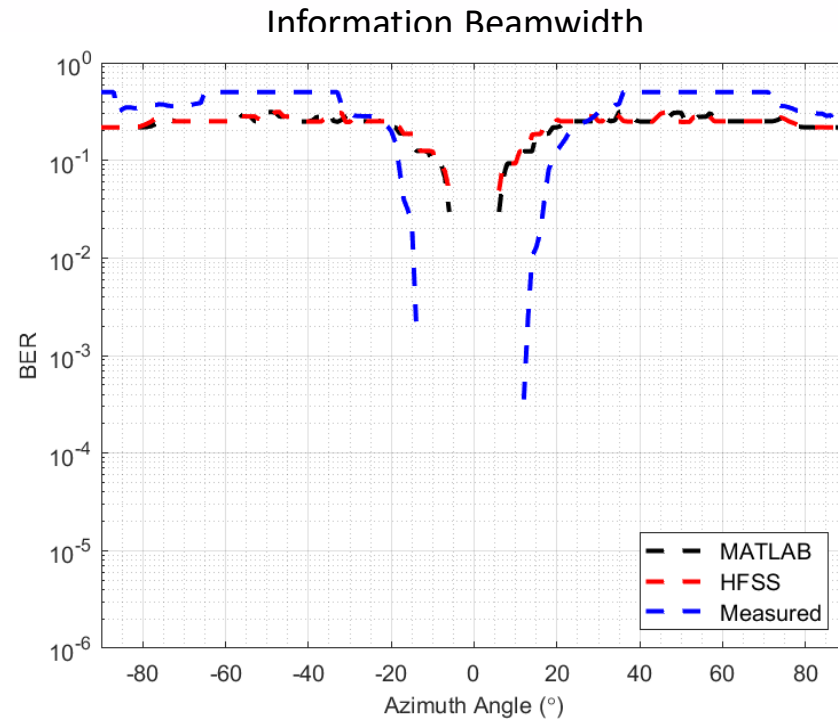
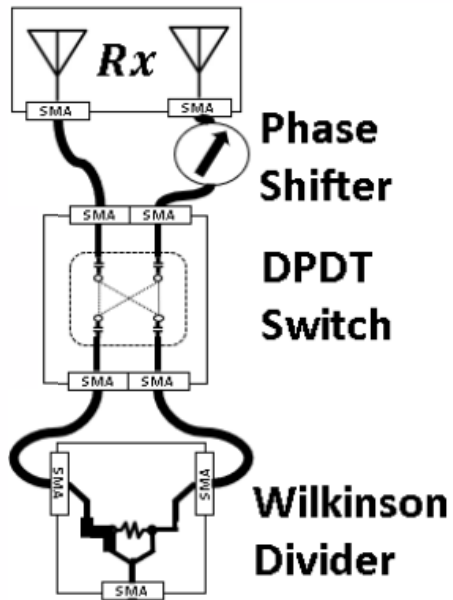
# Increased Distributed Fourier Domain Sampling



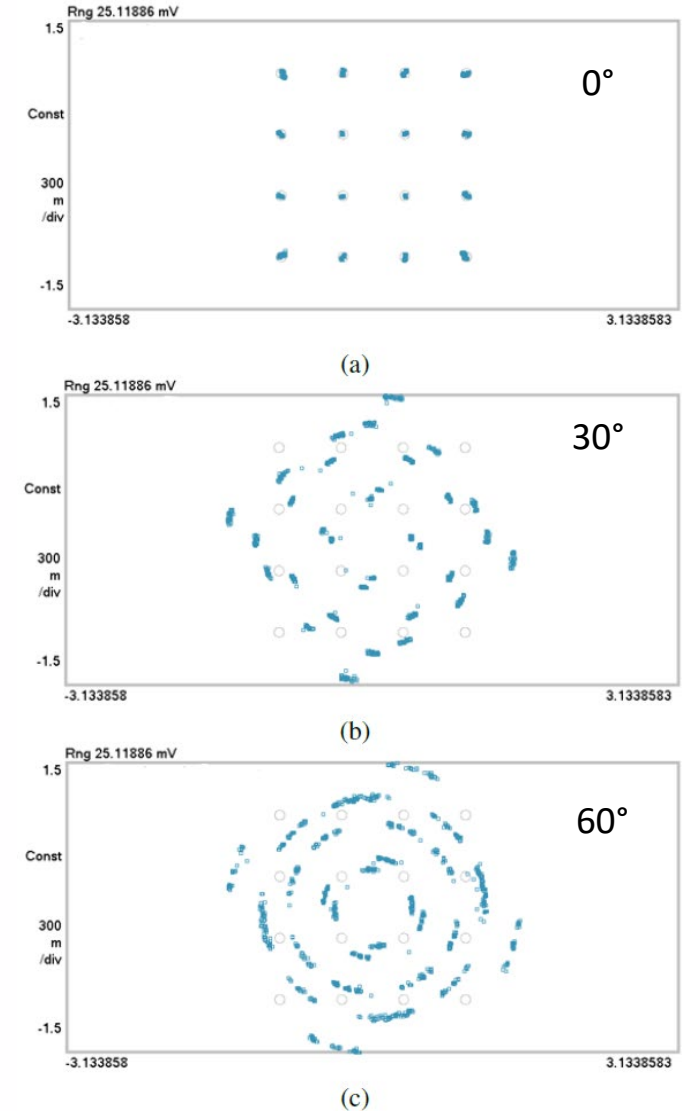
# Array Dynamics



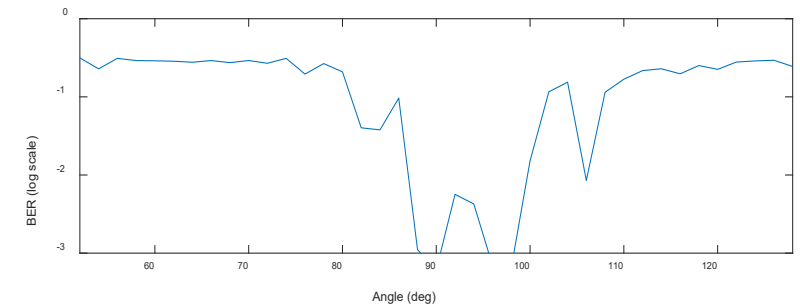
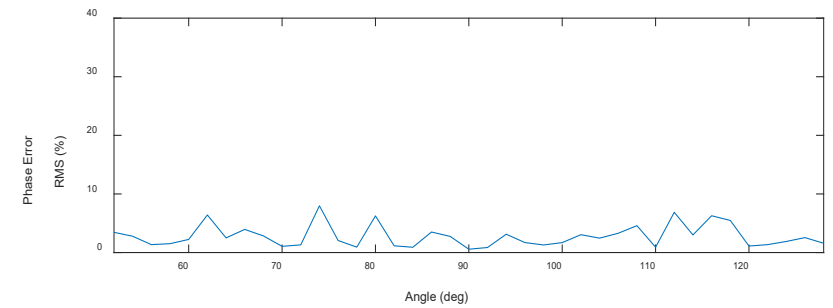
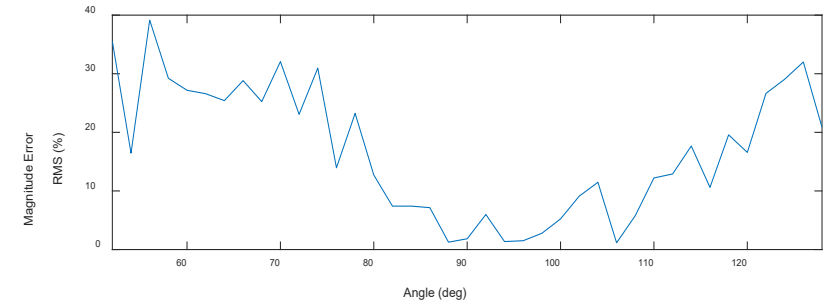
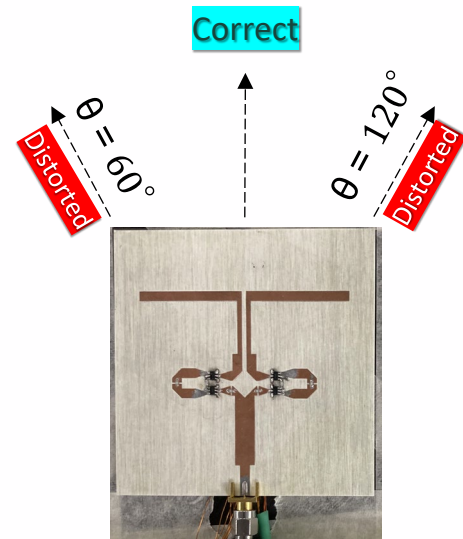
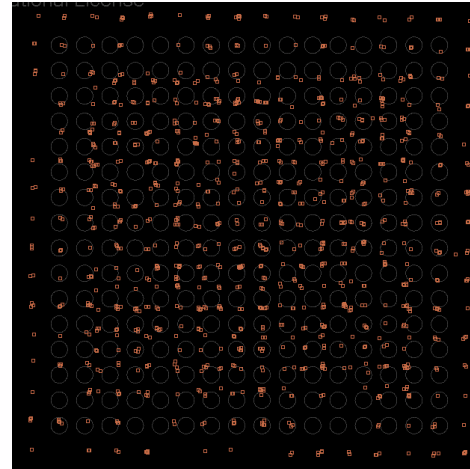
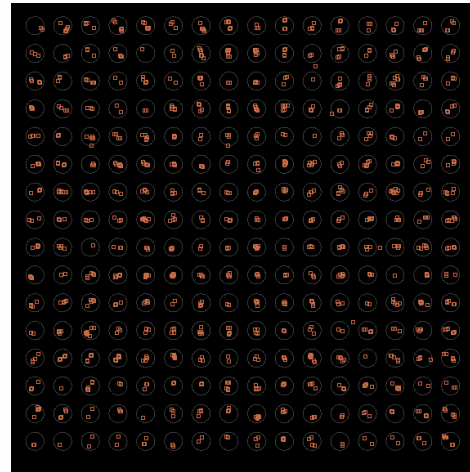
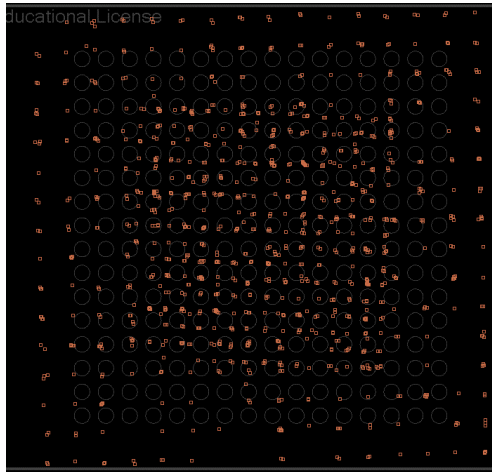
Dynamic amplitude/phase modulation in subarrays



Received data



# Single-Element Dynamics



# Summary



Microwave and millimeter-wave technologies have been developed to address the most fundamental challenges in coordinating distributed phased arrays

The unique nature of distributed phased arrays leaves possibilities for new measurement techniques and new directions of research