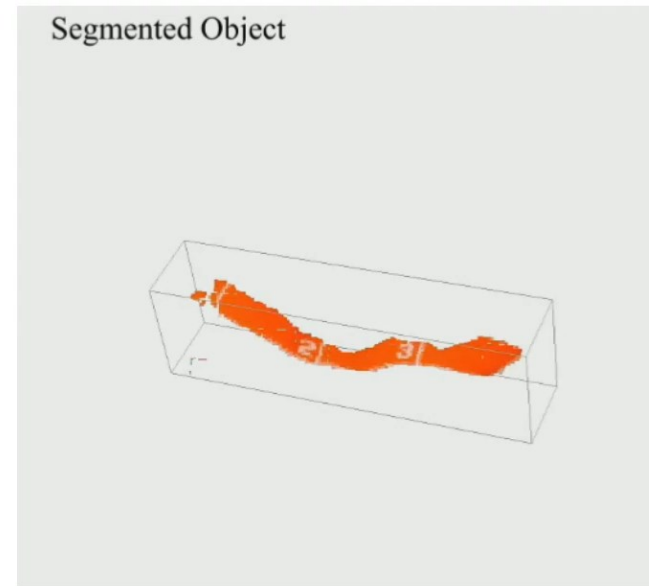
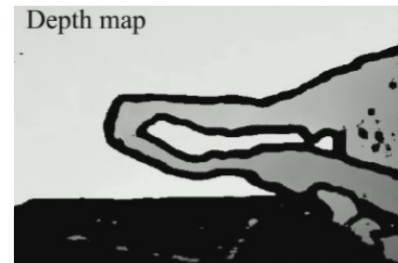


Data-driven manipulation and control of deformable objects

Ignacio Cuiral Zueco



Focus Period
Lund University
2025

Deformable object manipulation: a hot topic



Medical and surgical



Logistics, and transport



Automotive/aerospace industries



Food industry and agriculture

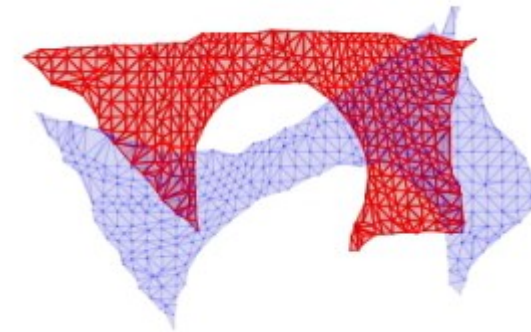
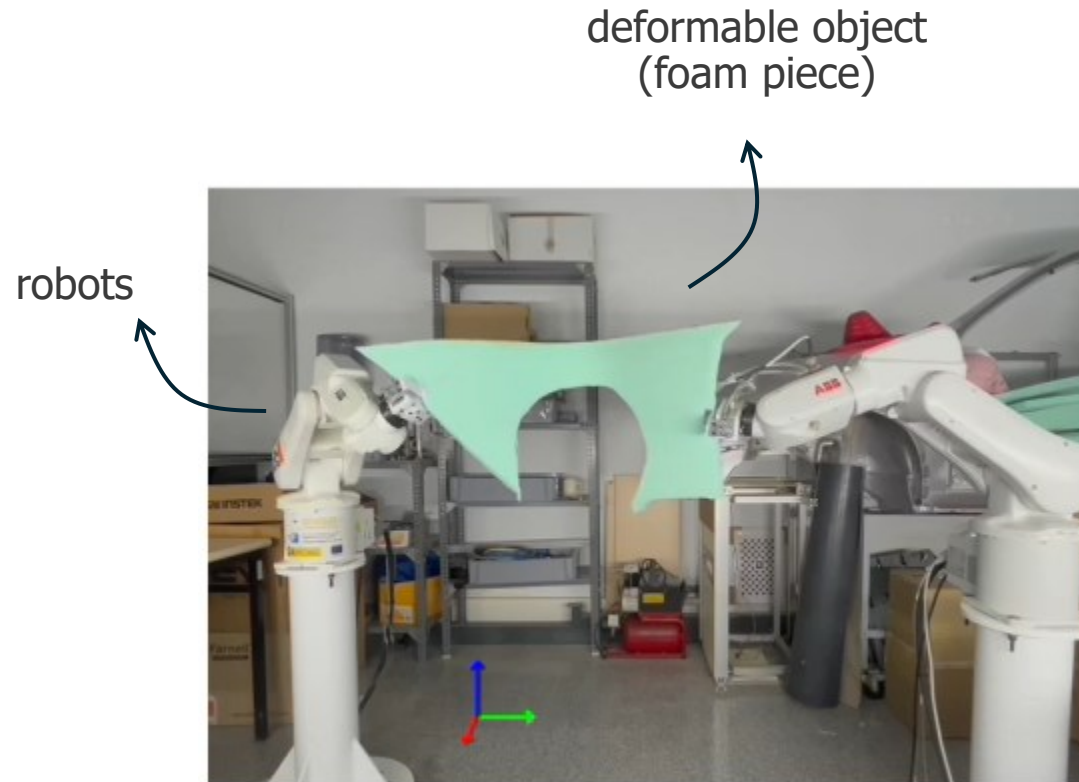


Electric industry/electronics



Textile and clothing industry

Central to deformable object manipulation: The shape control problem



initial shape
current shape
target shape

Objectives and structure

I. Introduction

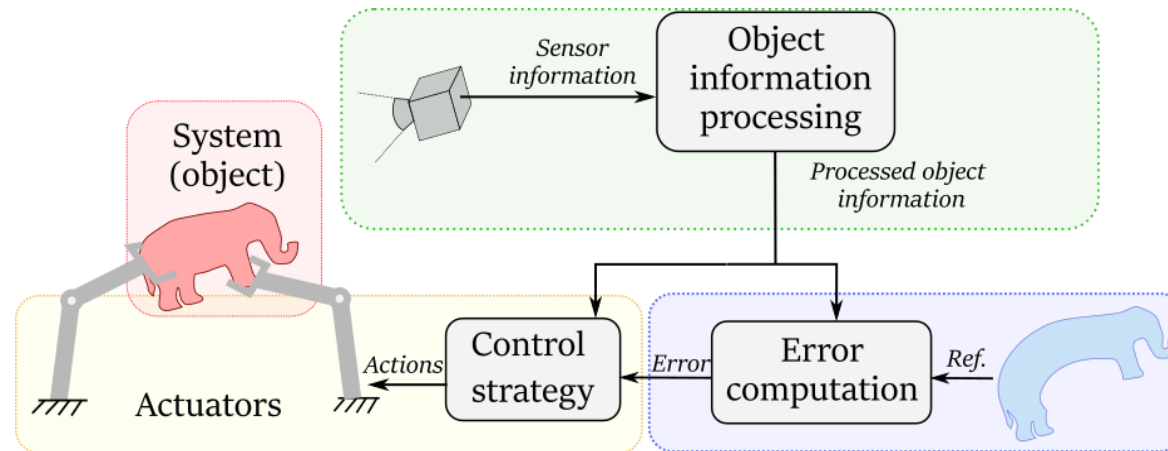
II. Deformable object perception

III. Shape as curve: mapping and control

IV. Shape as surface: mapping and control

V. Shape trajectory control

General goal: Enhance deformable object manipulation by developing advanced **perception**, **shape analysis**, and **control** techniques.



Cuiral-Zueco, I., et al., *IEEE Robotics and Automation Letters*, 2024.

Objectives and structure

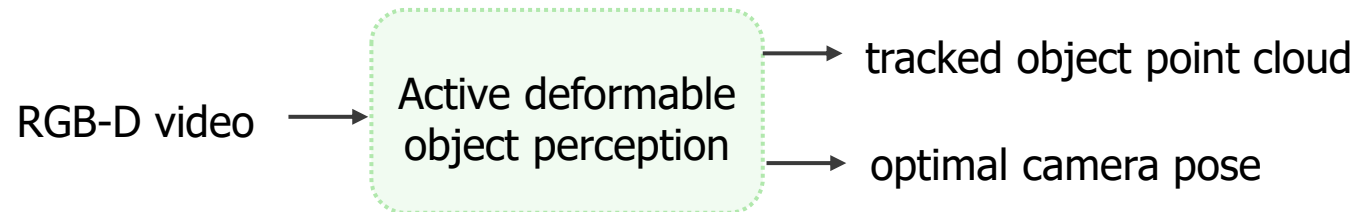
II. Deformable object perception

III. Shape as curve: mapping and control

IV. Shape as surface: mapping and control

V. Shape trajectory control

- Segment and track the object
- Locate camera pose
- Compute optimal camera pose for best perception



Active deformable object perception

Challenges

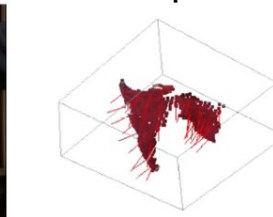
- Large deformations, and occlusions
- Lack of distinctive visual features
- Noisy/incomplete information

Our perception system:

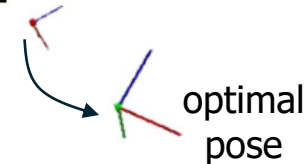
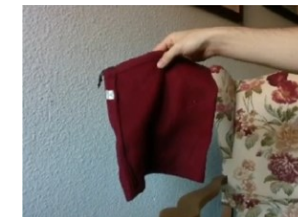
- Super-voxel dynamic graphs + SLAM
- C++ implementation
- Non-linear (online) Next-Best-View optimisation



Self-occluded object: ~20 supervoxels



With optimal pose: ~50 supervoxels



Cuiral-Zueco, I., et al., *IEEE Access*, 2020.

Cuiral-Zueco, I., et al., *IEEE ICRAE*, 2020.

Cuiral-Zueco, I., et al., Workshop, *IEEE IROS*, 2021.

Deformable object active perception results



Mop head manipulation



Paper tearing process

Cuiral-Zueco, I., et al., *IEEE Access*, 2020.

Cuiral-Zueco, I., et al., *IEEE ICRAE*, 2020.

Cuiral-Zueco, I., et al., Workshop, *IEEE IROS*, 2021.

Objectives and structure

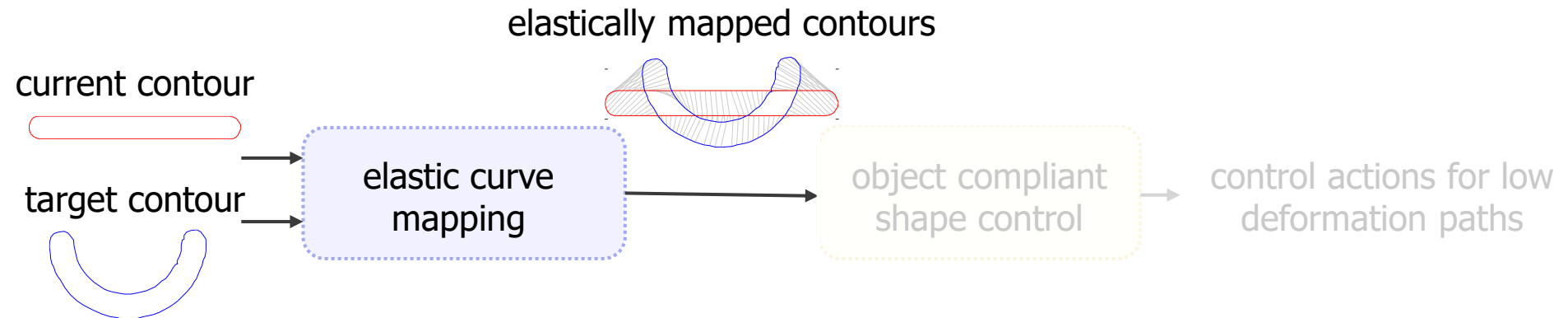
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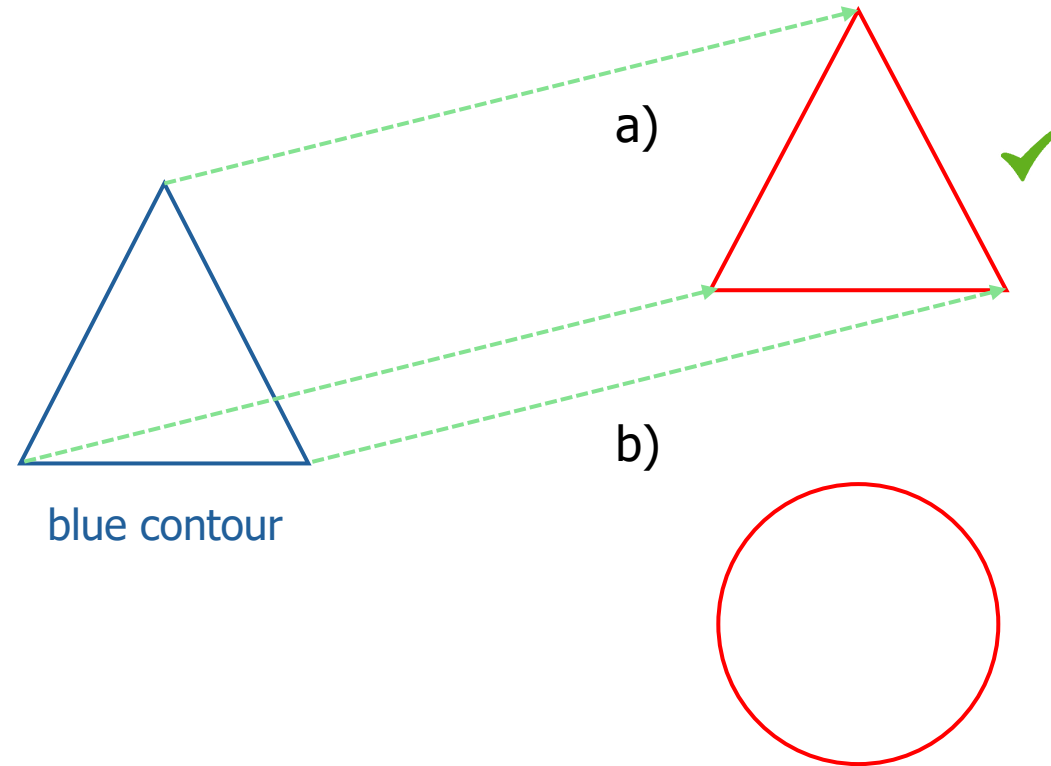
V. Shape trajectory control

- Map curves to infer realistic deformations between shapes
- *Gently* guide objects along low deformation paths



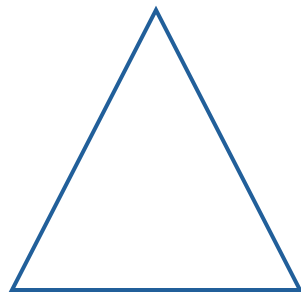
Shape comparison quiz

Level 1

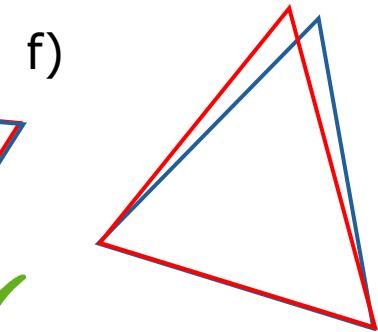
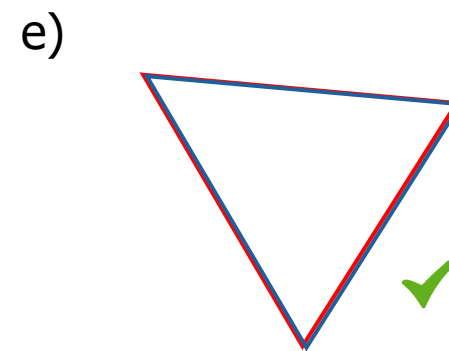
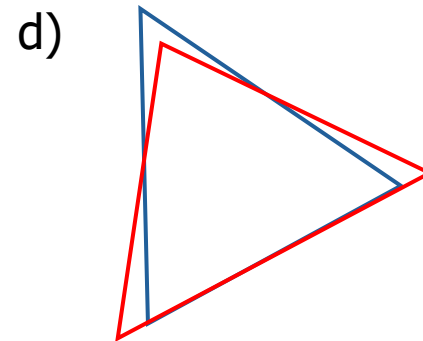
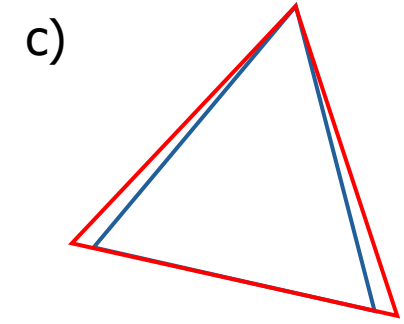
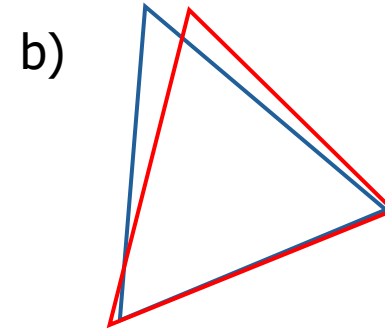
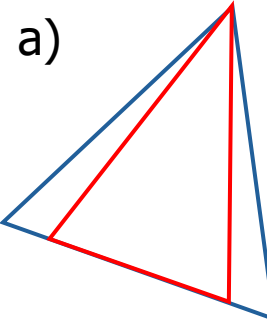


Shape comparison quiz

Level 2

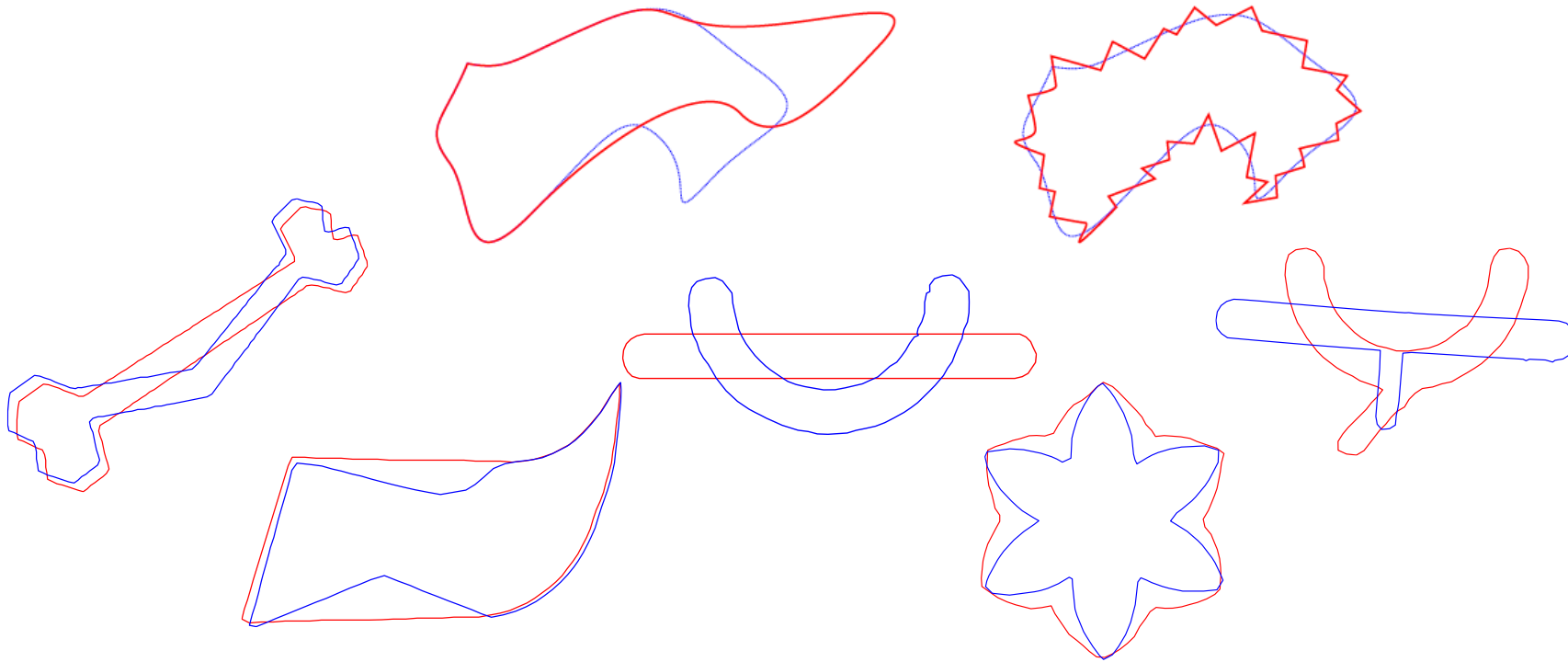


blue contour



Comparing shapes in an automatic, general, and measurable way is tricky

Comparing shapes (mapping domains) \approx deformation process estimation



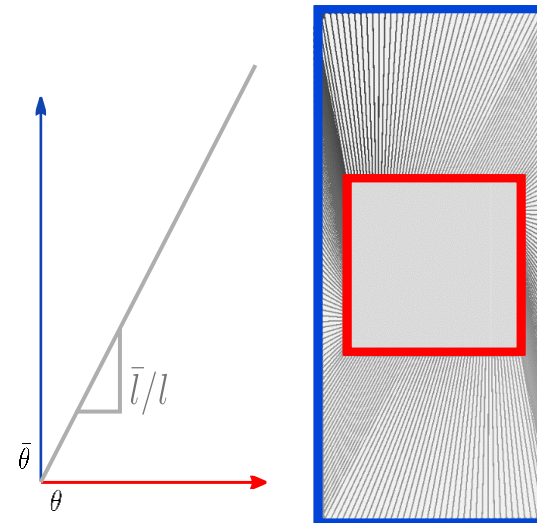
Elastic contour mapping

Challenges

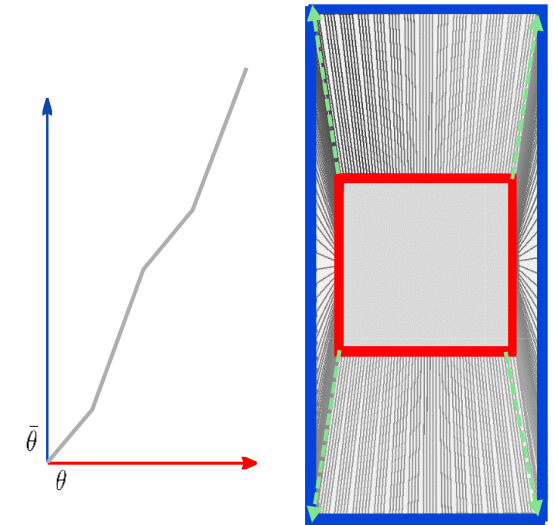
- No reference/landmark points
- Large and non-isometric deformation

Our elastic mapping:

- Favours geometry-preserving maps
- Proposed Multi-scale Laplacian descriptors
- Fast Marching Method (FMM) optimisation



*homogeneous map
(conventional approach)*



*elastic map
(ours)*

Elastic contour mapping

Challenges

- No reference/landmark points
- Large and non-isometric deformation

Our elastic mapping:

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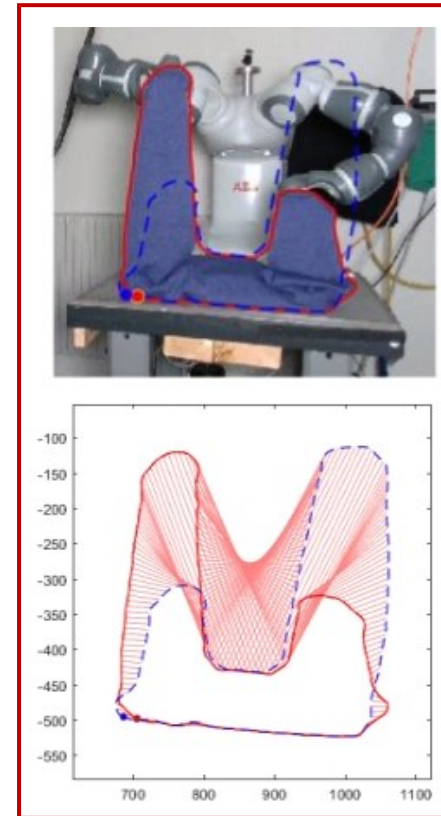
Cuiral-Zueco, I., et al., *IEEE ICRA*, 2022.

Cuiral-Zueco, I., et al., Workshop, *IEEE ICRA*, 2023.

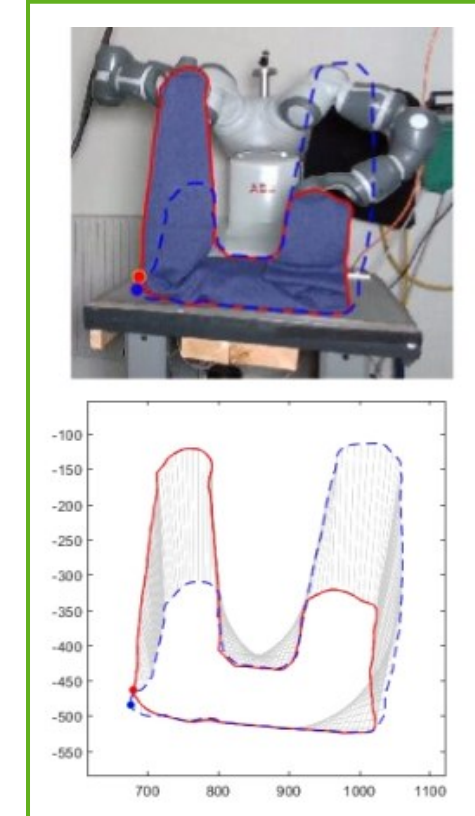
Cuiral-Zueco, I., et al., *IEEE Robotics and Automation Letters*, 2023.

Cuiral-Zueco, I., et al., *Lecture Notes in Networks and Systems*, Springer, 2024.

Cuiral-Zueco, I., et al., *Robotics and Autonomous Systems*, Springer, 2025.



homogeneous map
(conventional approach) ❌



elastic map
(ours) ✅

Control: Fourier-based deformation Jacobian estimation

Objectives and structure

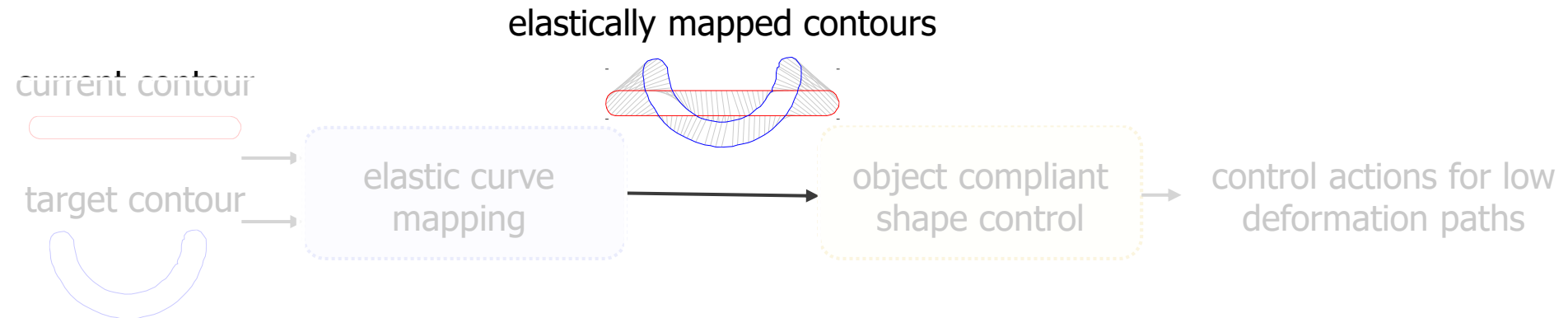
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- Map curves to infer realistic deformations between shapes
- *Gently* guide objects along low deformation paths



Object-compliant shape control

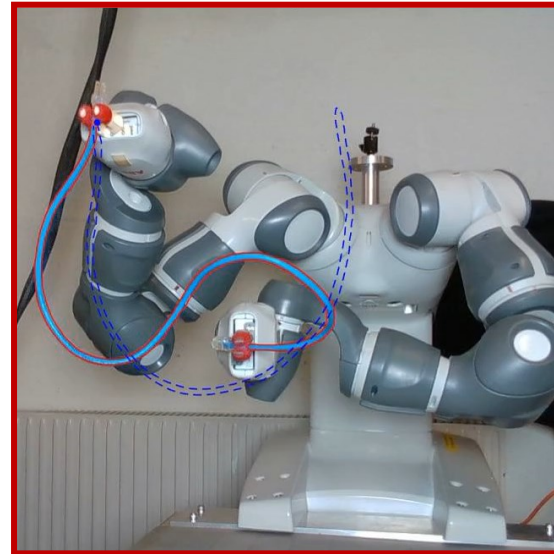
Challenges

- Object's have physical deformation limits
- We only have visual information

Our object-compliant control solution:

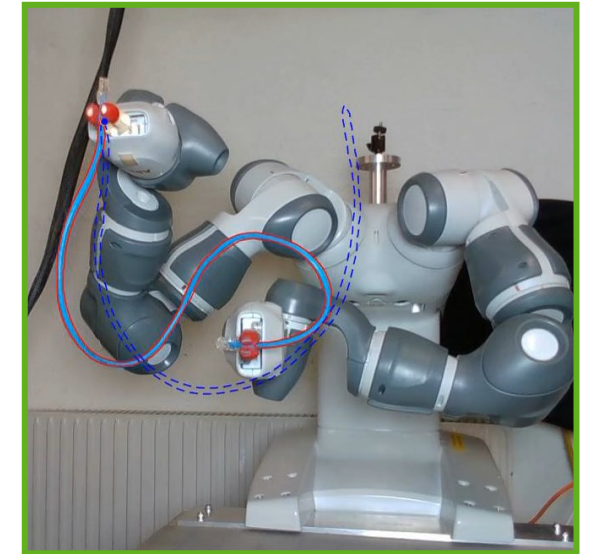
- Offline Jacobian estimation + online updates
- Exploits our elastic mapping
- Minimises joint intrinsic-extrinsic shape energy
- SE(2) invariant

Conventional shape control



high stress = risk to object ❌

Object-Compliant Shape Control



low deformation path ✅

Object: ethernet cable
Task: reach U-like shape

Cuiral-Zueco, I., et al., *IEEE ICRA*, 2022.

Cuiral-Zueco, I., et al., Workshop, *IEEE ICRA*, 2023.

Cuiral-Zueco, I., et al., *IEEE Robotics and Automation Letters*, 2023.

Cuiral-Zueco, I., et al., *Lecture Notes in Networks and Systems*, Springer, 2024.

Cuiral-Zueco, I., et al., *Robotics and Autonomous Systems*, Springer, 2025.

Objectives and structure

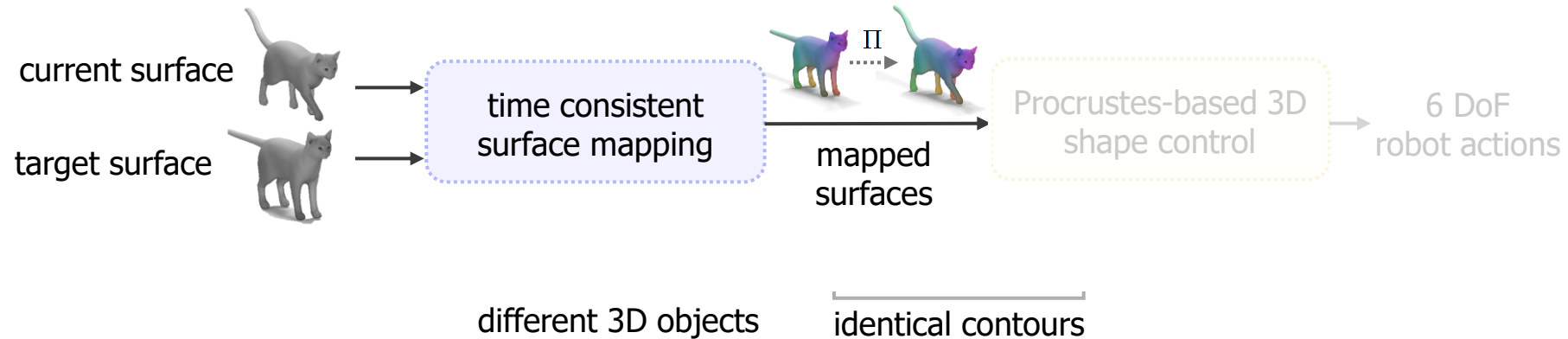
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- Map surfaces to infer realistic deformations
- Ensure consistent mapping through deformation process
- Control 3D shapes without offline object exploration
- Maintain robustness to singularities and disturbances



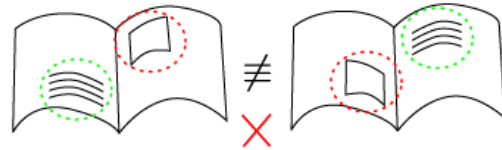
Shape as surface: shape comparison

Existing shape control methods compare surfaces through:

Visual features

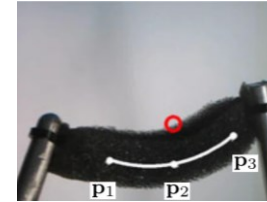


[M. Shetab-Bushehri et al., 2022]

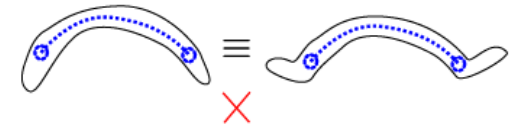


a) Not all objects have rich visual texture,
+ visual texture does not *mean* shape

Object-specific geometric features



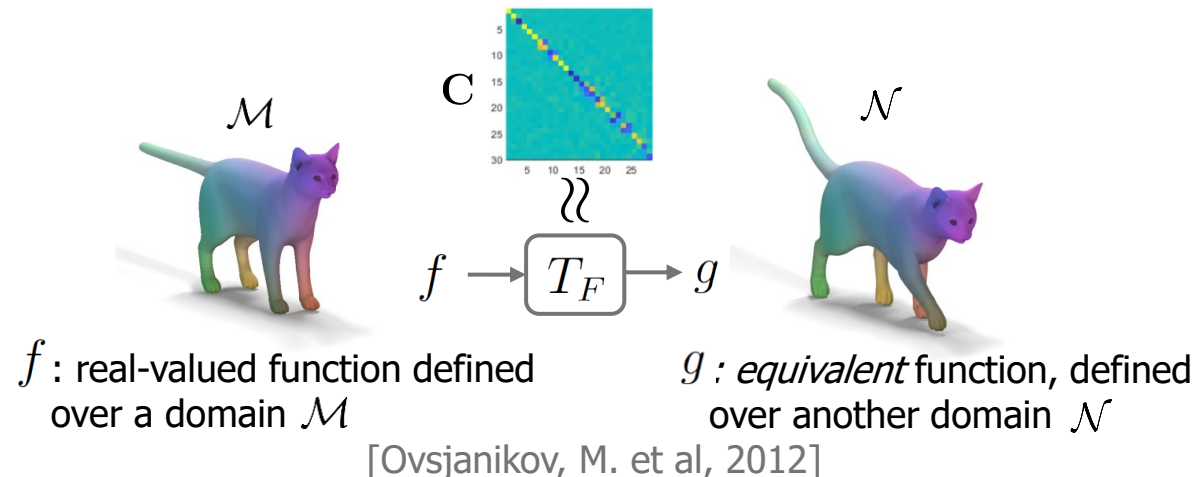
[D. Navarro-Alarcón et al., 2013]



b) poor generalization + parts of the
object are left out

Functional maps (computer graphics literature):

- Holistic static surface comparison
- No visual texture, pure shape analysis
- Can I just apply these methods to **non-ideal, time-evolving** meshes with **weak geometric features**, generated from **real, noisy sensor data**?



Time consistent surface mapping with functional maps

Challenges

- Noisy, texture-less point clouds
- Symmetries, deformations, *poor* geometry

Our time consistent surface mapping:

- Re-uses of low freq. Laplace eigenfunctions
- Keeps Eigen-basis sign consistent
- Robust to non-isometries

Target shape \mathcal{N}

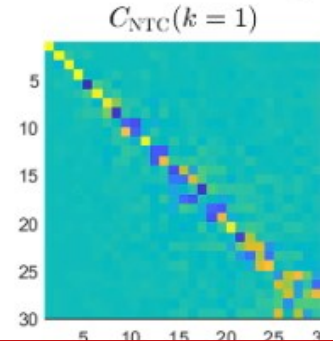


Current shape
 $\mathcal{M}(k=1), \Pi_{\text{NTC}}(k=1)$



inconsistent
ZoomOut
Method

Functional map
 $C_{\text{NTC}}(k=1)$

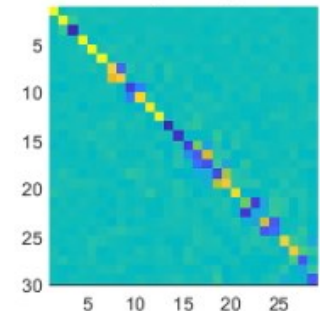


$\mathcal{M}(k=1), \Pi(k=1)$



time consistent
Ours

$C(k=1)$



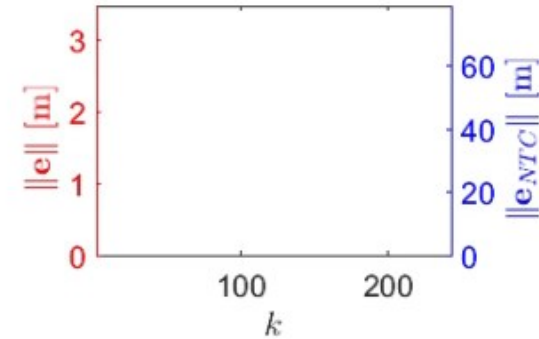
Object: hat

Time consistent surface mapping: shape control

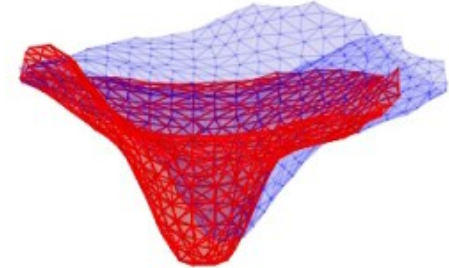
General camera view



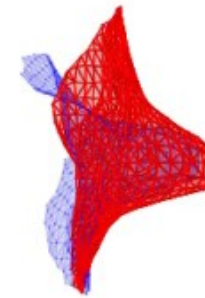
Our error /inconsistent error



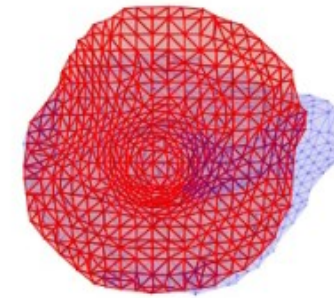
Top view



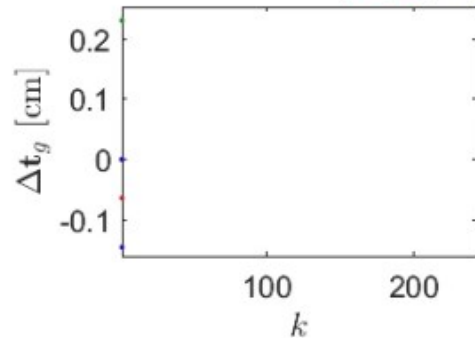
Side view



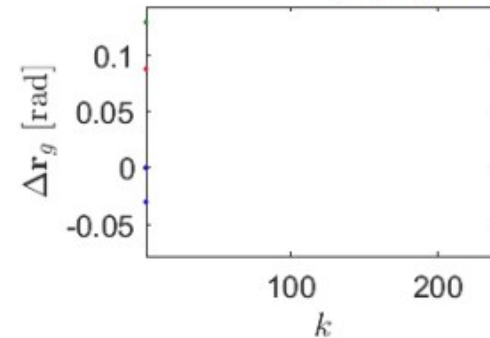
Front view



Translation (x , y , z)



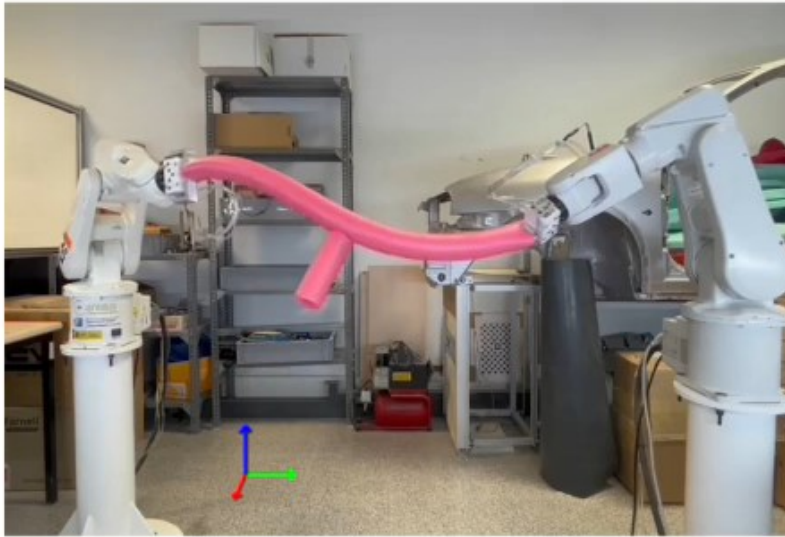
Rotation (r_x , r_y , r_z)



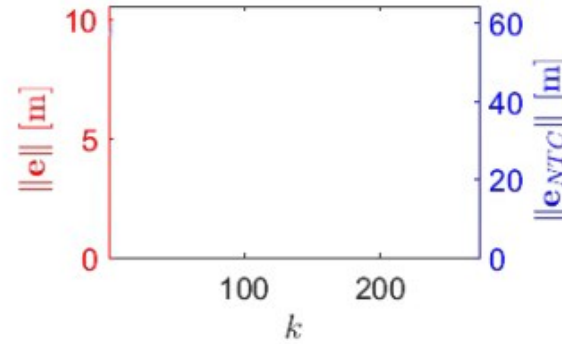
Initial state mesh: gray
Current state mesh: red
Target state mesh: blue

Time consistent surface mapping: shape control

General camera view



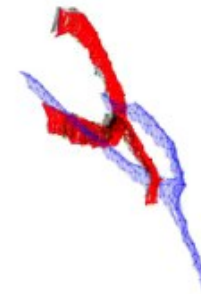
Our error / inconsistent error



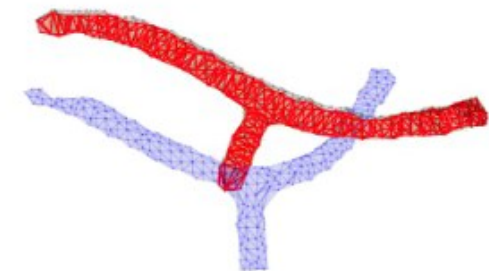
Top view



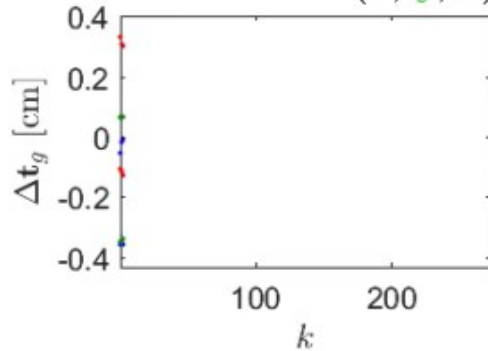
Side view



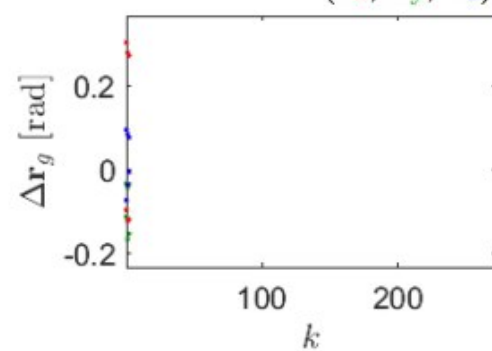
Front view



Translation (x, y, z)



Rotation (r_x, r_y, r_z)



Initial state mesh: gray
Current state mesh: red
Target state mesh: blue

Deformation Jacobian: offline estimated and online updated

Objectives and structure

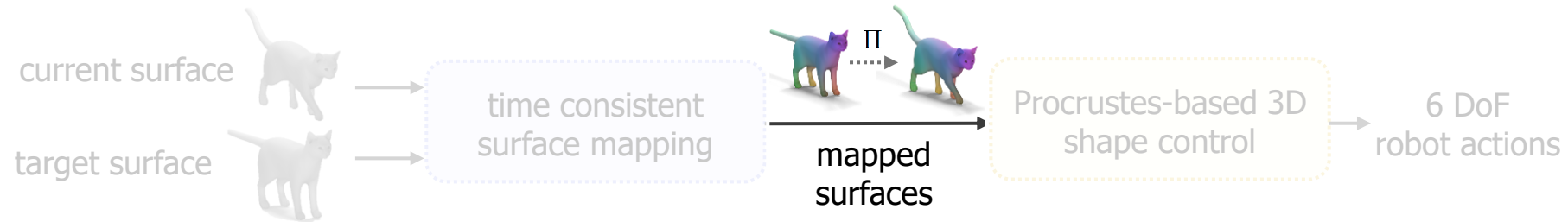
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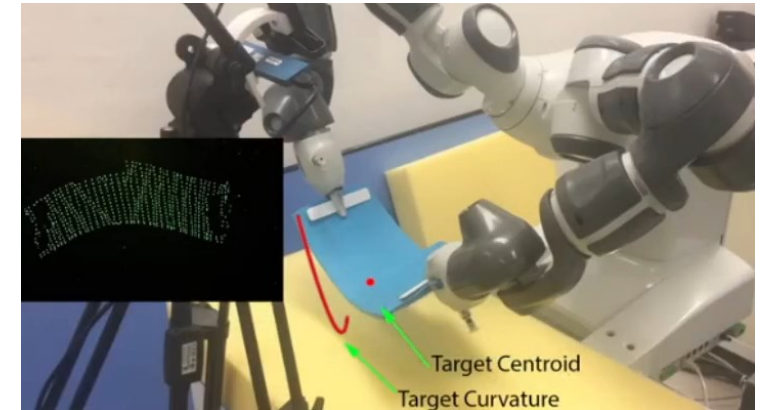
- Map surfaces to infer realistic deformations
- Ensure consistent mapping through deformation process
- Control 3D shapes without offline object exploration
- Maintain robustness to singularities and disturbances



3D shape control of surfaces

Existing surface control approaches

- Few analysed features \Rightarrow incomplete shape control
[Hu et al., 2018 , M Shetab-Bushehri et al., 2022]
- Offline object exploration \Rightarrow impractical for industrial processes
[Navarro-Alarcon et al., 2016; Hu et al., 2018]



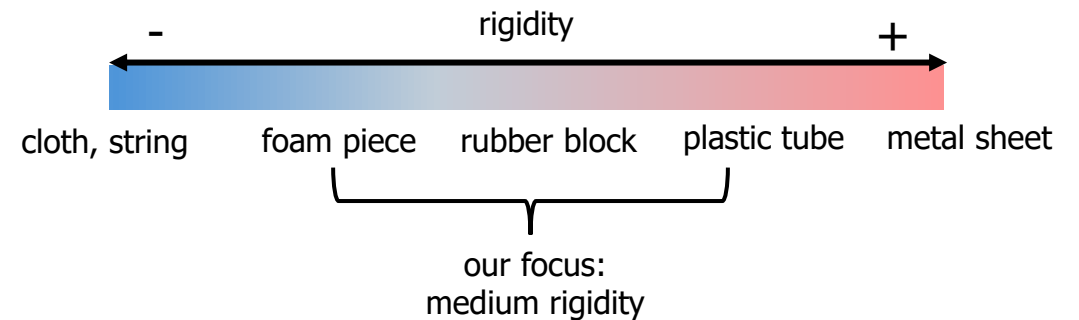
[Hu et al., 2018]

Our goals

- Control entire object geometry
- Online process: no offline object exploration
- Robust against singularities and disturbances

However

- Achieving these goals for all object types is unrealistic



Procrustes-based 3D shape control

Challenges

- Control entire object geometry
- Offline object behaviour exploration \Rightarrow impractical

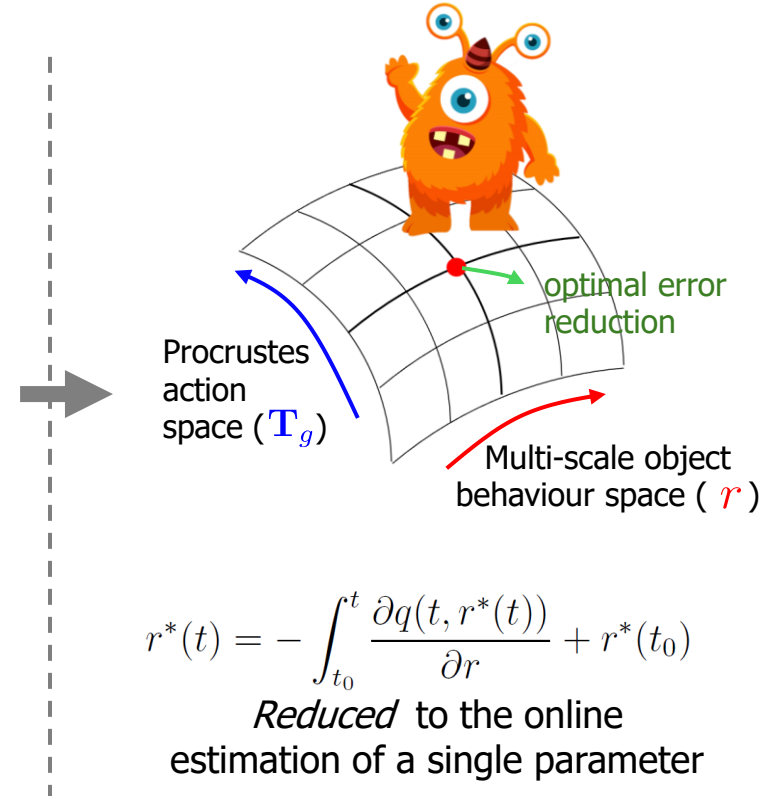
Our 3D surface shape online control:

- Exploits time consistent surface mapping
- Optimisation in $SE(3)$, Procrustes geodesics
- Lyapunov stability (local)

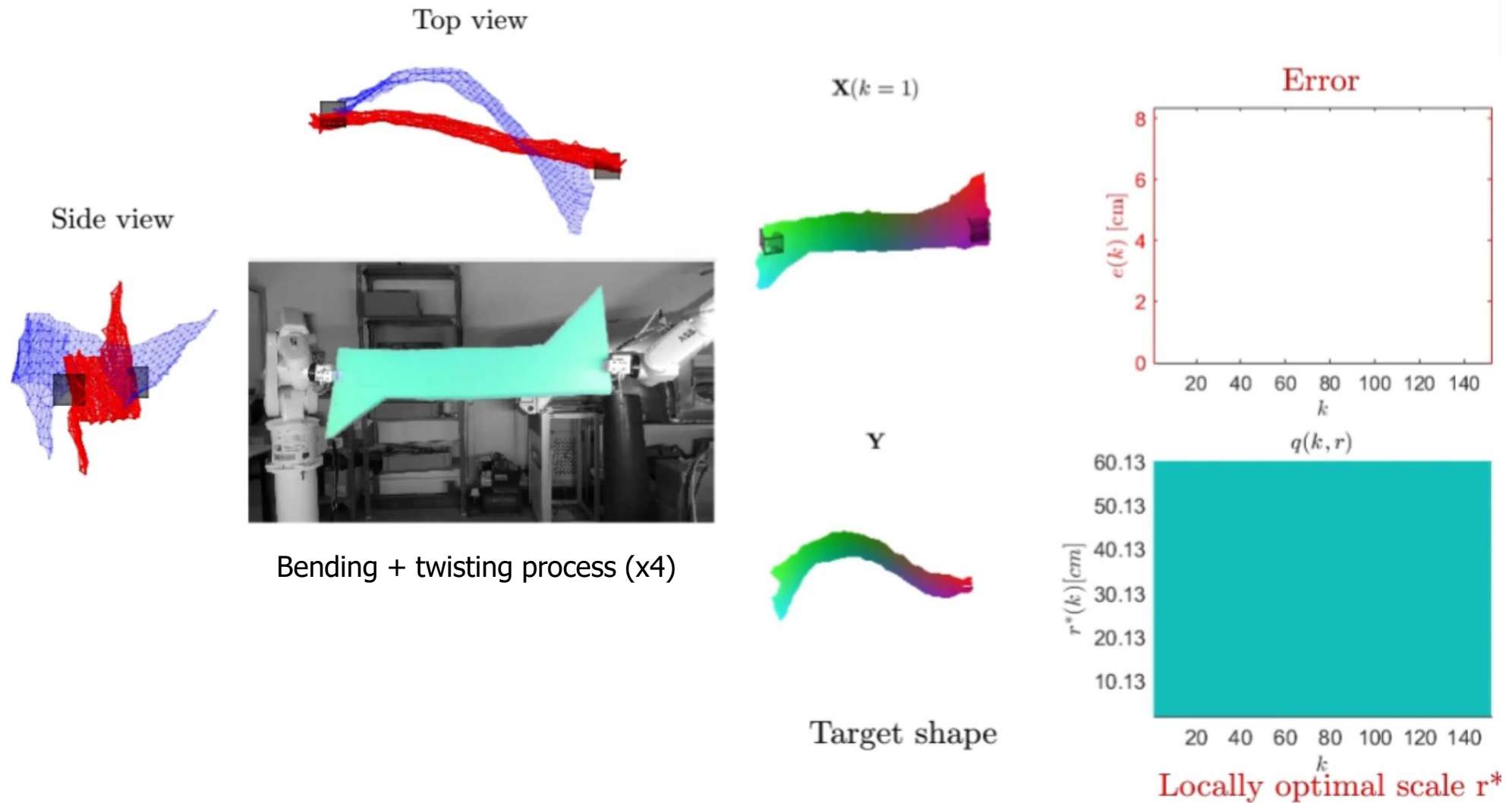


$$\frac{dx}{dt} = f(x(t), u(t))$$

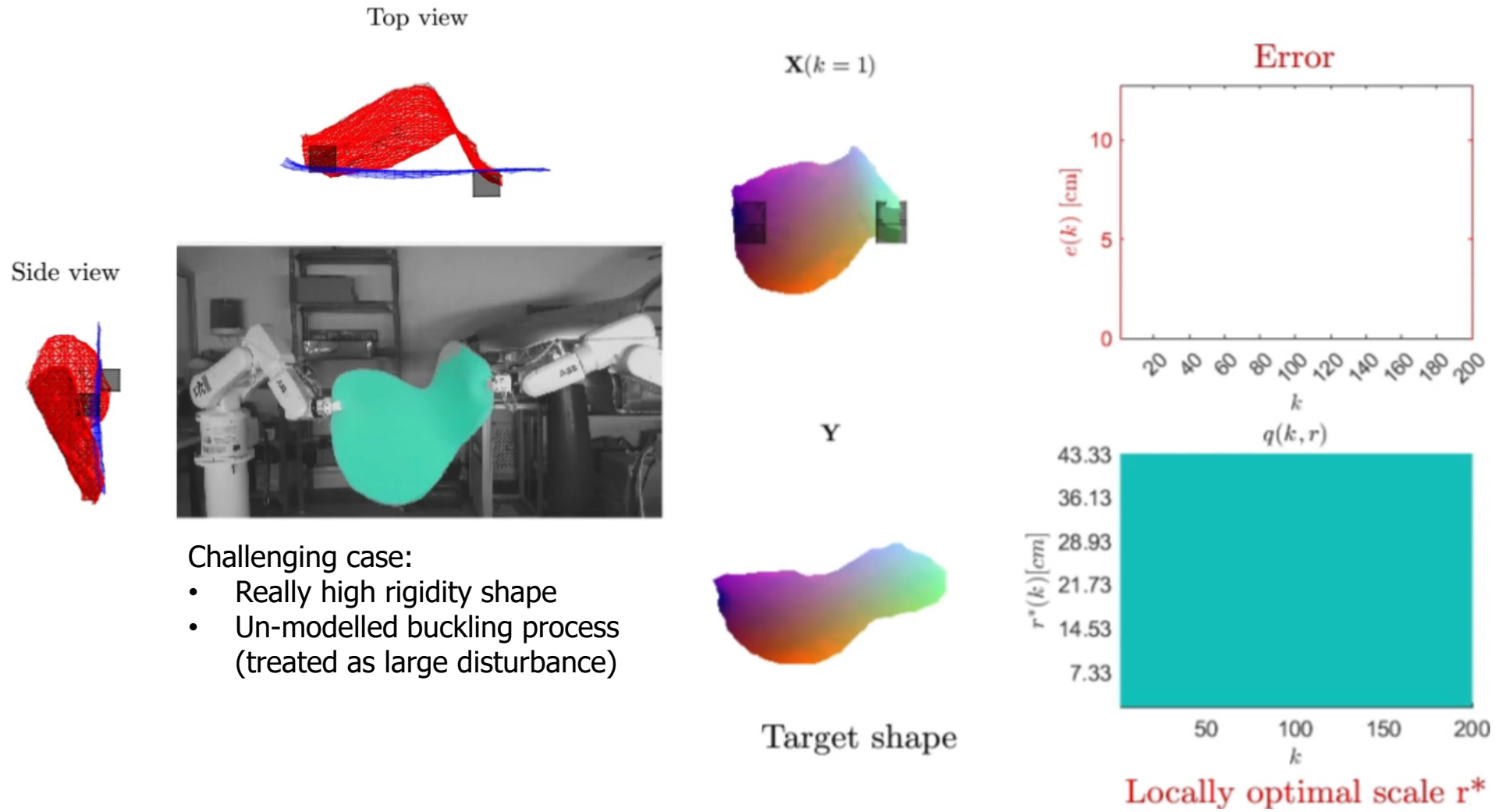
*infinitely dimensional,
underactuated nonlinear system*



Procrustes-based 3D shape control: results



Procrustes-based 3D shape control: results



Objectives and structure

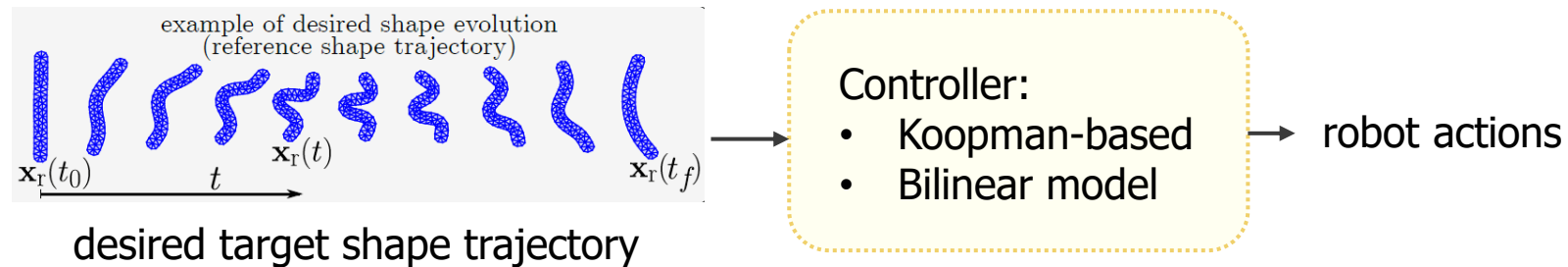
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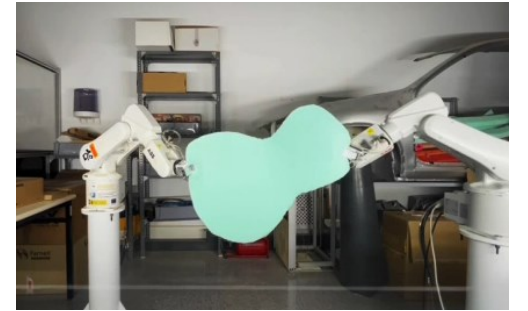
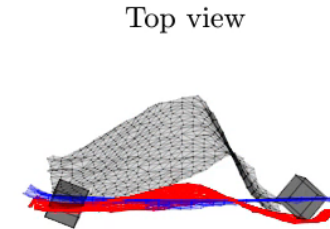
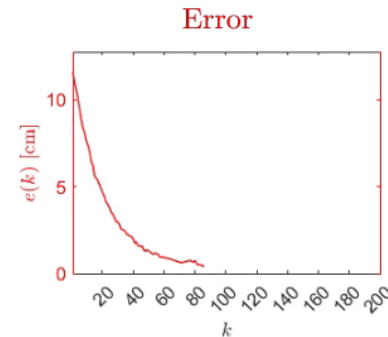
- Use time-varying shape evolution as control reference
- Predict and control non-quasistatic responses
- Stability and reachability analysis



Shape trajectory control

Challenges

- Model and control non-quasistatic behaviour
- *Highly* non-linear



Our Procrustes control: rejected the buckling *disturbance* but did not predict it

Our shape trajectory control system

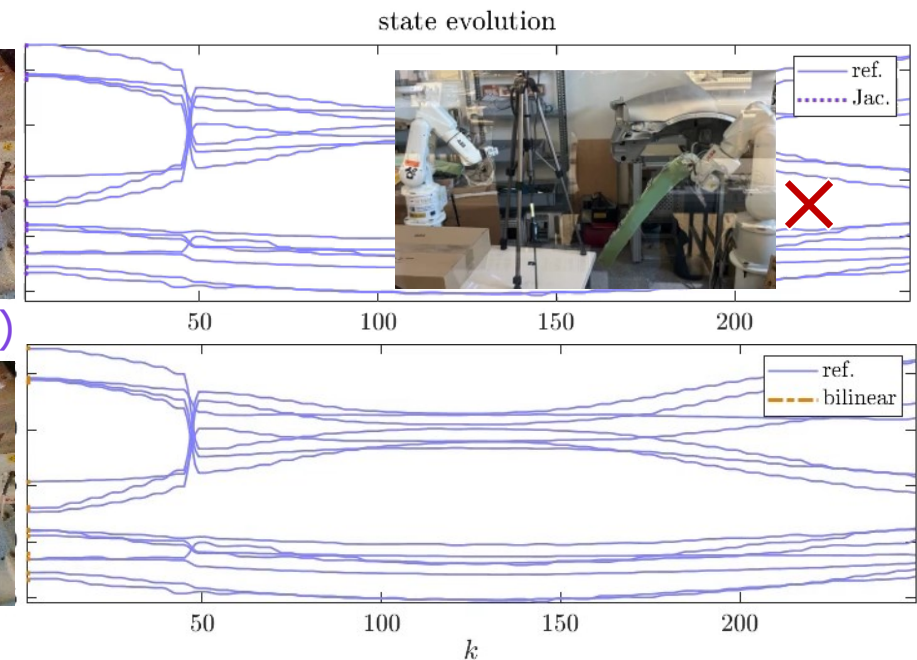
- SINDY (Sparse Identification of Non-linear Dynamics)
- Koopman and Bilinear models
- Lie algebra transitivity analysis (reachable space) + Global uniform ultimate boundedness (GUUB)



Jacobian (conventional)



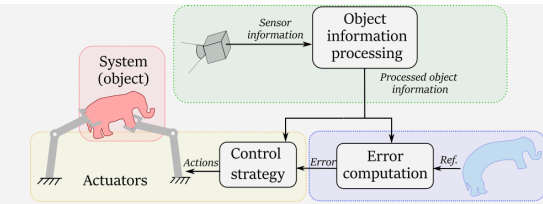
Bilinear (ours)



So far...

Taxonomy for deformable object shape control:

1. First taxonomy in the literature.



Optimal deformable object perception:

2. Active perception system with Next Best View and occlusion avoidance.



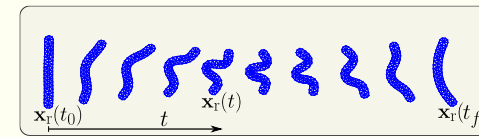
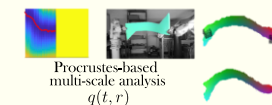
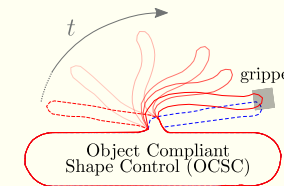
Holistic shape analysis and comparison from real data (contours and surfaces)

3. Multi-scale elastic contour mapping (FMM, Laplacian descriptors).
4. Time-consistent surface mapping (Functional Maps).



Novel shape control methods for deformable object

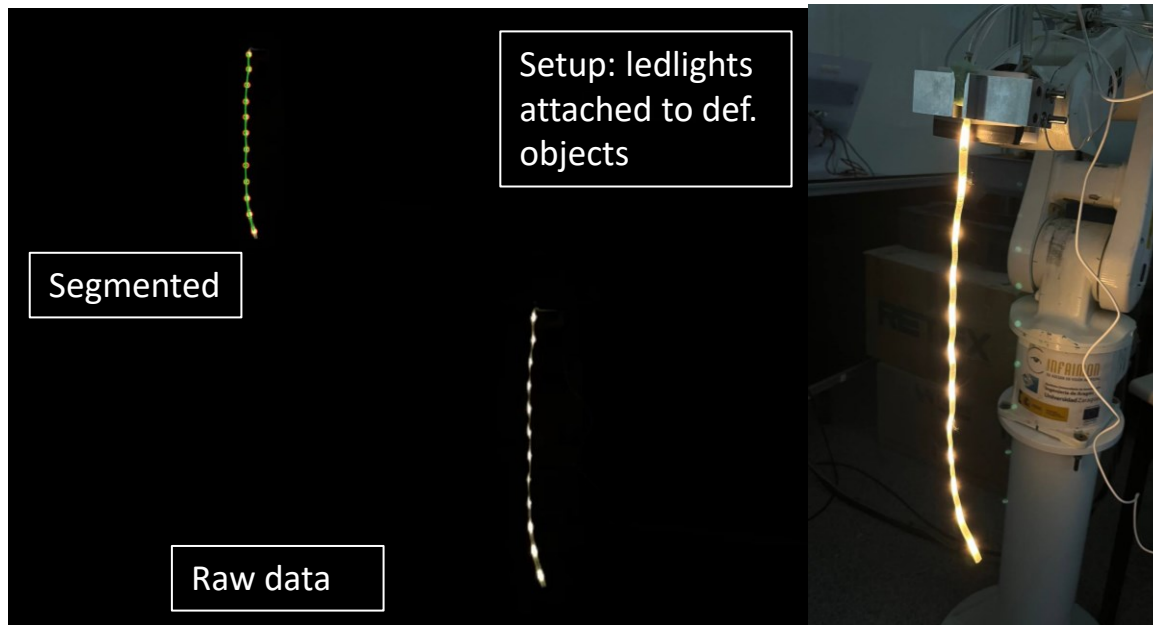
5. Contour-based Object-Compliant Shape Control (OCSC).
6. Pure-online Procrustes-based surface shape control.
7. Shape Trajectory Control: Koopman and Bilinear formulations.



+ automatic gripper positioning method, and abrupt deformation estimation method

What's next? (1/3)

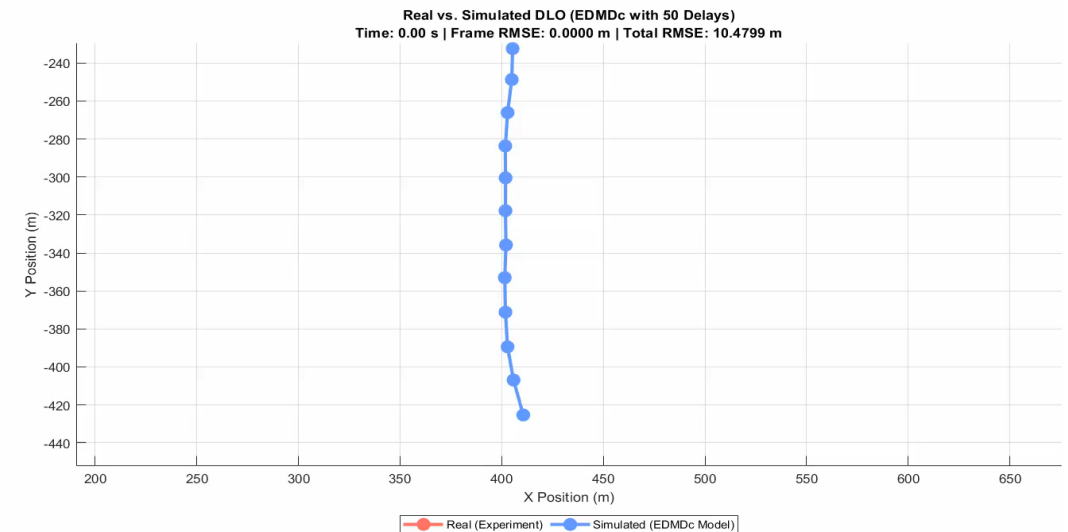
- Identification and control of highly dynamic systems (the *not-so-pleasantly* quasi-static kind)



*Groundtruth data obtention of object material points
240 fps, otherwise, motion blur ruins segmentation*

Promissing directions...

- Extended Dynamic Mode Decomposition + Control
- Order reduction to achieve real-time nonlinear MPC just from robot hand sensor data (not vision dependent)



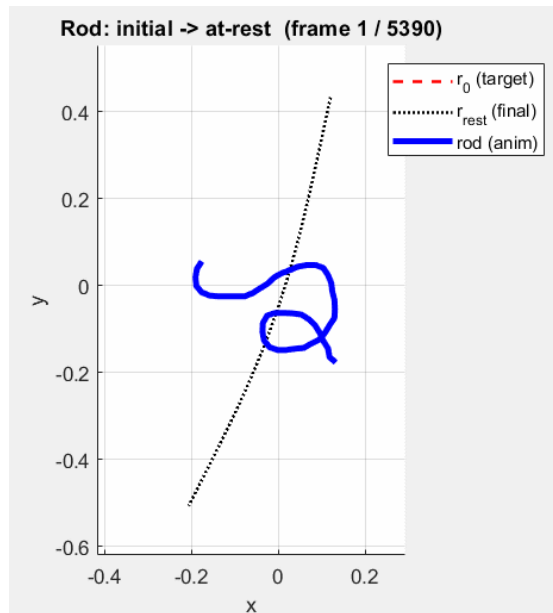
DMDC (with delays) open-loop estimation

What's next? (2/3)

- Task-oriented feasible target shape definition
 - In all the experiments we saw, target shapes were defined by pre-acquiring the object state as a snapshot
 - Defining task-relevant target shapes (planning) that are compliant with the object AND the robot system... seems interesting

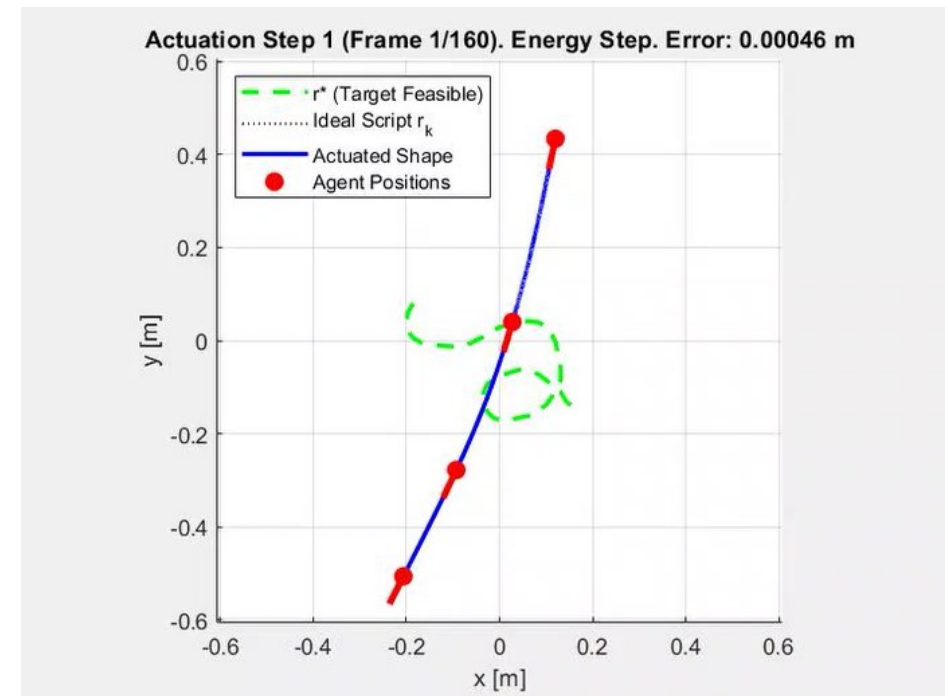
Promising directions...

- Cosserat rod model variational analysis + optimal grasping point definition
- Force-based control, impedance-based control



Free-rod relaxation from arbitrary target shape

*Physical-feasibility analysis
(strain limits) + agent-pose
optimisation*



*Shape control with
4 agents*

What's next? (3/3)

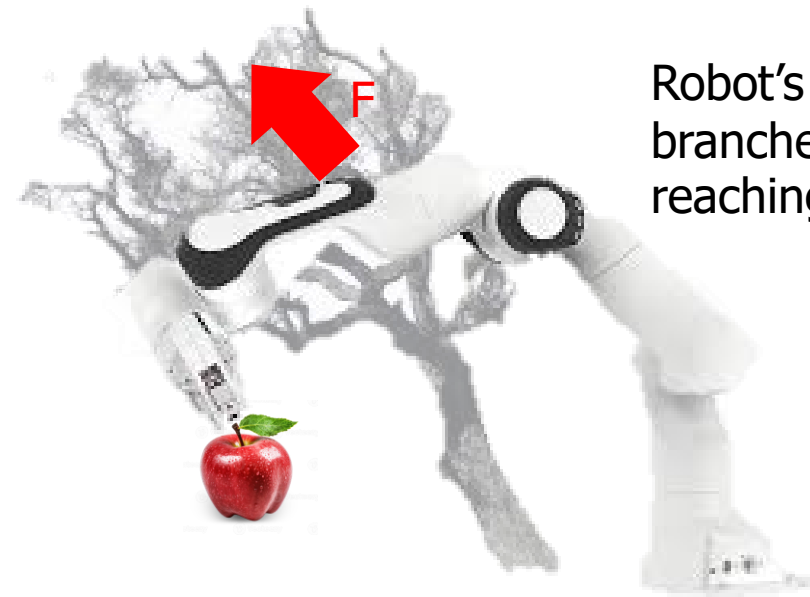
- Non-prehensile multi-contact (whole-body) manipulation
 - Coordinating Prehensile and Non-Prehensile Contacts
 - With particular focus in agriculture (but generalizable to other manufacturing processes)
 - Basically pushing obstacles away while manipulating other objects

Promising directions...

- Impedance-based control, virtual force analysis
- Cosserat rod model + friction-cone definition and control (CBFs?) to avoid slippage



*Occluded fruits
(branches = obstacles)*



Robot's elbow pushes branches away while reaching for the apple

Presentation based on these publications (first author):

Journals:

1. *RGB-D Tracking and Optimal Perception of Deformable Objects*, **IEEE Access**, 2020.
2. *Contour-Based Object-Compliant Shape Control*, **IEEE RA-L**, 2023.
3. *Taxonomy of Deformable Object Shape Control*, **IEEE RA-L**, 2024.
4. *Deformable Object Shape Trajectory Control with Data-Driven Models*, **IEEE/ASME T-MECH** ([under review](#)).
5. *Multiscale Procrustes-Based 3D Shape Control*, **IEEE/ASME T-MECH**, 2024.
6. *Time-Consistent Surface Mapping for Shape Control*, **IEEE T-ASE**, 2025.
7. *Multi-Scale Elastic Contour Mapping for Shape Control*, **ELSEVIER RAS**, 2025.

Conference Papers:

1. *Gripper Positioning for Object Deformation Tasks*, **ICRA**, 2022.
2. *Multi-Scale Laplacian-Based FMM for Shape Control*, **IROS**, 2021.
3. *Dynamic Occlusion Handling for Real-Time Object Perception*, **ICRAE**, 2020.
4. *Elastic Contour Mapping for Estimation of Abrupt Shape Deformations*, **ROBOT**, 2023.

Workshops:

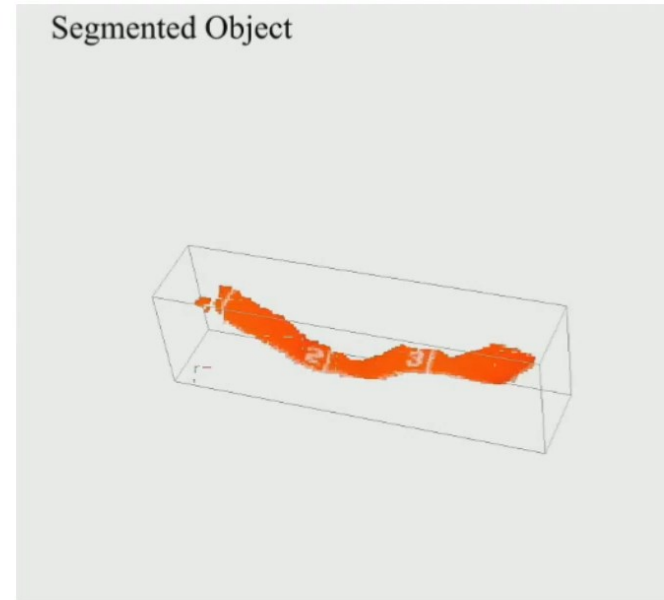
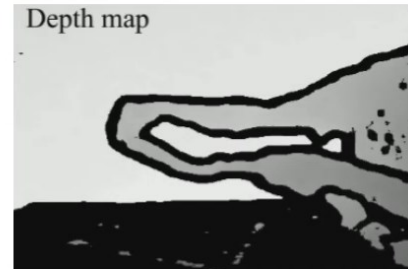
1. *RGB-D Sensing of Challenging Deformable Objects*, Workshop on Managing Deformation, **IROS** 2020.
2. *Mesh Estimation for Abrupt Deformations of Texture-Less Objects*, Workshop on Representing and Manipulating Deformable Objects, **ICRA** 2023.

Data-driven manipulation and control of deformable objects

Thanks!



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Experiment videos

General research interests: to develop novel techniques for the **perception, shape analysis, and control** of deformable objects.